

Intro to Rational Expressions

Fractions and Exponents Review

Fractions Review

Adding and Subtracting Fractions

Always find a common denominator when adding or subtracting fractions!

$$\text{a) } \frac{1^{\cancel{x}4}}{2^{\cancel{x}4}} + \frac{1}{8}$$

$$= \frac{4}{8} + \frac{1}{8}$$

$$= \frac{5}{8} \text{ (keep denominator)}$$

$$\text{b) } \frac{2x^{\cancel{x}2}}{3y^{\cancel{x}2}} - \frac{y^{\cancel{x}3y}}{2^{\cancel{x}3y}}$$

*common denom = 3y(2)
= 6y*

$$= \frac{4x}{6y} - \frac{3y^2}{6y}$$

$$= \frac{4x - 3y^2}{6y}$$

Multiplying and Dividing Fractions

You do NOT need a common denominator when multiplying or dividing fractions!

a) $\frac{3}{2} \cdot \frac{4}{5}$

$$= \frac{(3)(4)}{(2)(5)}$$

$$= \frac{12}{10}$$

$$= \frac{6}{5}$$

b) $\frac{2}{3} \div \frac{4}{3}$

*Flip second
* fraction and *
multiply*

$$= \frac{2}{3} \times \frac{3}{4}$$

$$= \frac{6}{12}$$

$$= \frac{1}{2}$$

Rule: We can NEVER have a fraction with a denominator of 0. Why?

eg. $\frac{6}{2} = 3$

why? because $2 \times 3 = 6$

$$\left\{ \frac{6}{0} = ? \right.$$

This means $0 \times \underline{\quad} = 6$

Rule: Cross multiplication of fractions only happens when..... *There is an = sign between two fractions.*

eg. $\frac{2}{3} = \frac{x}{5}$

$$5(2) = 3x$$

$$10 = 3x$$

$$x = \frac{10}{3}$$

Rule: We can cancel out ONLY when multiplying fractions

You can cancel factors.

$$\begin{array}{l} \text{eg. } \frac{\cancel{x}(x+1)}{\cancel{x}} = x+1 \\ \text{eg. } \frac{3\cancel{x}(x+3)}{2\cancel{4x}} = \frac{3x+9}{2} \end{array} \left. \vphantom{\begin{array}{l} \text{eg. } \frac{\cancel{x}(x+1)}{\cancel{x}} = x+1 \\ \text{eg. } \frac{3\cancel{x}(x+3)}{2\cancel{4x}} = \frac{3x+9}{2} \end{array}} \right\} \begin{array}{l} \text{These are} \\ \text{examples of} \\ \text{when cancelling} \\ \text{is allowed.} \end{array}$$

Rule: We can NOT cancel out when adding or subtracting fractions

$$\text{eg. } \frac{\cancel{x}+8}{\cancel{x}} \quad \underline{\underline{\text{NO!}}} \quad \text{Don't do this!}$$

$$\text{eg. } \frac{2x+3}{4x} \quad \leftarrow \text{No cancelling!}$$

Name	Rule	Examples
Adding and Subtracting Monomials	COMBINE LIKE TERMS! (do not change common variables and exponents)	$3x^2y + 2x^2y =$ $5x^2y$
Product Rule	$x^a \cdot x^b = x^{a+b}$	$(-2x^2y)(3x^3y^2) =$ $-6x^5y^3$
Quotient Rule	$\frac{x^a}{x^b} = x^{a-b}$	$\frac{28x^5}{42x} = \frac{2x^4}{3}$
Power of a Power Rule	$(x^a)^b = x^{a \cdot b}$	$(-2x^3)^2 =$ $4x^6$
Negative Exponent Rule	$x^{-a} = \frac{1}{x^a}$	$\frac{4x^2}{8x^5} = \frac{1}{2x^3}$
Exponent of Zero	$x^0 = 1$	$87^0 =$ 1

Simplify the following rational expressions using exponent laws

a)
$$\frac{12k^2m^8}{4k^5m^5} = 3k^{-3}m^3$$

$$= \frac{3m^3}{k^3}$$

b)

$$\frac{5c^3d \cdot 4c^2d^2}{(2c^2d)^2} = \frac{20c^5d^3}{4c^4d^2}$$
$$= 5cd$$

c)

$$\frac{(3xy)^3}{9x^4y^4} = \frac{27x^3y^3}{9x^4y^4}$$
$$= 3x^{-1}y^{-1}$$
$$= \frac{3}{xy}$$

d)

$$\begin{aligned}\frac{(2z^3)^{-2}}{w^5 z^2} &= \frac{2^{-2} z^{-6}}{w^5 z^2} \\ &= \frac{1}{2^2 w^5 z^2 z^6} \\ &= \frac{1}{4w^5 z^8}\end{aligned}$$

e)

$$\begin{aligned}\frac{(x^{-4})^5 x^3}{3x^{-1}} &= \frac{x^{-20} x^3}{3x^{-1}} \\ &= \frac{x^{-17}}{3x^{-1}} \\ &= \frac{1}{3x^{-1} x^{17}} \\ &= \frac{1}{3x^{16}}\end{aligned}$$

Combining fractions and exponents:

$$\begin{aligned}\text{ex. } & \frac{3x^{\cancel{1}}}{2\cancel{x}} + \frac{4y^{\cancel{3}}}{3\cancel{y}} \\ & = \frac{3x^{\times 3}}{2^{\times 3}} + \frac{4y^{\cancel{3} \times 2}}{3^{\times 2}} \\ & = \frac{9x}{6} + \frac{8y^3}{6} \\ & = \frac{9x+8y^3}{6}\end{aligned}$$

COMPLETE WORKSHEET

Intro to Rational exponents (Fractions):

$$\sqrt[2]{x^1}$$

bottom
(also called the index)

top

radicand.

$$= x^{\frac{1}{2}}$$

Powers with a rational exponent of the form $\frac{1}{n}$

A power involving a rational exponent with numerator 1 and denominator n can be interpreted as the n th root of the base:

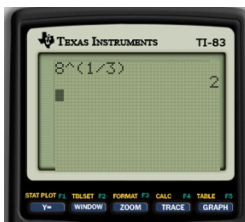
$$b^{\frac{1}{n}} = \sqrt[n]{b}$$

Powers with a rational exponent of the form $\frac{1}{n}$

Example 1: Evaluate each of the following

a) $8^{\frac{1}{3}}$

$= 2$



b) $\sqrt[5]{-32}$

$= (-32)^{\frac{1}{5}}$

$= -2$

c) $-16^{\frac{1}{4}}$

$= -2$

d) $\sqrt[4]{\frac{16}{81}}$

$= \left(\frac{16}{81}\right)^{\frac{1}{4}}$

$= \frac{(16)^{\frac{1}{4}}}{(81)^{\frac{1}{4}}}$

$= \frac{2}{3}$

e) $(-27)^{-\frac{1}{3}}$

$= \frac{1}{(-27)^{\frac{1}{3}}}$

$= \frac{1}{-3}$

$= -\frac{1}{3}$

Powers with a rational exponent of the form $\frac{m}{n}$

You can evaluate a power involving a rational exponent with numerator m and denominator n by taking the n th root of the base raised to the exponent m :

$$b^{\frac{m}{n}} = (\sqrt[n]{b})^m = \sqrt[n]{b^m}$$

Powers with a rational exponent of the form $\frac{m}{n}$

Example 2: Simplify each of the following powers

a)

$$\sqrt[5]{y^2}$$

$$= y^{\frac{2}{5}}$$

b)

$$\sqrt[3]{x}$$

$$= x^{\frac{1}{3}}$$

$$\begin{aligned} \text{c) } & \sqrt{a^{-3}b^{\frac{4}{3}}} \\ &= (a^{-3}b^{\frac{4}{3}})^{\frac{1}{2}} \\ &= a^{-3/2}b^{4/6} \\ &= \frac{b^{2/3}}{a^{3/2}} \end{aligned}$$

$$\begin{aligned} \text{d) } & \sqrt[4]{x^3y^2} \\ &= (x^3y^2)^{1/4} \\ &= x^{3/4}y^{2/4} \\ &= x^{3/4}y^{1/2} \end{aligned}$$

$$\begin{aligned} \text{e) } & \frac{\sqrt[3]{x^2yy^2}}{x^3} \\ &= \frac{(x^2y)^{1/3}y^2}{x^3} \\ &= \frac{x^{2/3}y^{1/3}y^{6/3}}{x^3} \\ &= x^{-7/3}y^{7/3} \\ &= \frac{y^{7/3}}{x^{7/3}} \end{aligned}$$

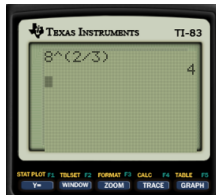
Example 3: Evaluate each of the following

a) $8^{\frac{2}{3}}$

$$= (8^{\frac{1}{3}})^2$$

$$= (2)^2$$

$$= 4$$



b) $81^{\frac{5}{4}}$

$$= (81^{\frac{1}{4}})^5$$

$$= (3)^5$$

$$= 243$$

c) $\left(\frac{49}{81}\right)^{-\frac{3}{2}}$

$$= \left(\frac{81}{49}\right)^{3/2}$$

$$= \frac{(81)^{3/2}}{(49)^{3/2}}$$

$$= \frac{729}{343}$$

If you have a power with a negative exponent and a rational base, just flip the base and make the exponent positive.

Apply Exponent Rules

Example 4: Simplify and express answer using only positive exponents

a)

$$\frac{\left(x^{\frac{2}{3}}\right)\left(x^{\frac{2}{3}}\right)}{\left(x^{\frac{1}{3}}\right)} = \frac{x^{\frac{4}{3}}}{x^{\frac{1}{3}}}$$
$$= x^{\frac{3}{3}}$$
$$= x$$

b)

$$\left(y^{\frac{1}{4}}\right)^2 \times \left(y^{-\frac{1}{3}}\right)^2$$
$$= y^{\frac{1}{2}} \times y^{-\frac{2}{3}}$$
$$= y^{\frac{3}{6}} \times y^{-\frac{4}{6}}$$
$$= y^{-\frac{1}{6}}$$
$$= \frac{1}{y^{\frac{1}{6}}}$$

c)

$$\left(5x^{\frac{1}{2}}\right)^2 \times 4x^{-\frac{1}{2}}$$

$$= 25x \cdot 4x^{-\frac{1}{2}}$$

$$= 25x^{\frac{2}{2}} \cdot 4x^{-\frac{1}{2}}$$

$$= 100x^{\frac{1}{2}}$$

d)

$$\frac{(m^{-2})^3 \sqrt{m^4}}{m \sqrt{pq^{-3}}}$$

$$= \frac{m^{-6} \cdot m^{\frac{4}{2}}}{m p^{\frac{1}{2}} q^{-\frac{3}{2}}}$$

$$= \frac{m^{-6} \cdot m^2}{m p^{\frac{1}{2}} q^{-\frac{3}{2}}}$$

$$= \frac{m^{-4}}{m p^{\frac{1}{2}} q^{-\frac{3}{2}}}$$

$$= \frac{m^{-5}}{p^{\frac{1}{2}} q^{-\frac{3}{2}}}$$

$$= \frac{q^{\frac{3}{2}}}{m^5 p^{\frac{1}{2}}}$$

e)

$$\frac{(x^2)^{-4} \sqrt[5]{y^3}}{y \sqrt{x^{-2} y}}$$

$$= \frac{x^{-8} y^{3/5}}{y x^{-1} y^{1/2}}$$

$$= \frac{x^{-7} y^{3/5}}{y^{3/2}}$$

$$= \frac{x^{-7} y^{6/10}}{y^{15/10}}$$

$$= x^{-7} y^{-9/10}$$

$$= \frac{1}{x^7 y^{9/10}}$$

Complete Worksheet

2.1/2.2 Restricting, Simplifying, Multiplying, and Dividing Rational Expressions

Lesson Outline:

Part 1: Stating restrictions

Part 2: Simplifying rational expressions

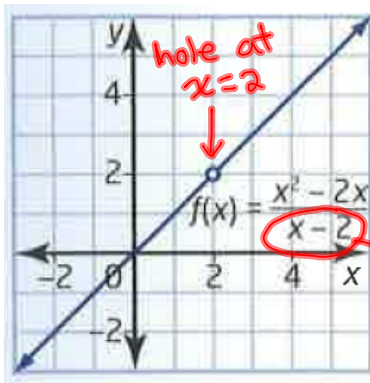
Part 3: Multiplying rational expressions

Part 4: Dividing rational expressions

What is a rational expression?

Rational expression: the quotient of two polynomials, $\frac{p(x)}{q(x)}$, where $q(x) \neq 0$.

Example of a graph of a rational expression:



The open circle is used to represent a hole in the graph. This corresponds to any restrictions on the variable (denominator can't be 0).

$$x - 2 \neq 0$$
$$x \neq 2$$

Stating Restrictions

Note: rational expressions must be checked for restrictions by determining where the denominator is equal to **zero**. These restrictions must be stated when the expression is simplified.

bottom of a fraction can
NOT = 0.

Example 1: State the restrictions for the following rational expressions

a)

$$\frac{x+2}{x-2}$$
$$x-2 \neq 0$$
$$x \neq 2$$

$x \neq 2$

b)

$$\frac{x+2}{(x-3)(x+4)}$$
$$x-3 \neq 0$$
$$x \neq 3$$
$$x+4 \neq 0$$
$$x \neq -4$$

$x \neq 3, -4$

c)

$$\frac{5}{x(x+3)}$$
$$x \neq 0$$
$$x+3 \neq 0$$
$$x \neq -3$$

$x \neq 0, -3$

Rule: We can cancel out **ONLY** when multiplying fractions

You can cancel factors.

$$\text{eg. } \frac{\cancel{x}(x+1)}{\cancel{x}} = x+1$$

$$\text{eg. } \frac{3\cancel{x}(x+3)}{24\cancel{x}} = \frac{3x+9}{2}$$

These are examples of when cancelling is allowed.

Rule: We can **NOT** cancel out when adding or subtracting fractions

$$\text{eg. } \frac{\cancel{x}+8}{\cancel{x}} \quad \underline{\underline{\text{NO!}}} \quad \text{Don't do this!}$$

$$\text{eg. } \frac{2x+3}{4x} \quad \text{No cancelling!}$$

Simplifying Rational Expressions

Example 2: Simplifying each expression and determine any restrictions on the variable.

a) $\frac{3x^{\cancel{2}1}}{y\cancel{x}}$, $y \neq 0$
 $x \neq 0$

$$= \frac{3\cancel{x}}{y} , \begin{matrix} y \neq 0 \\ x \neq 0 \end{matrix}$$

b) $\frac{x-3}{x^2+3x-18}$

Note: factor where possible and then state restrictions before cancelling factors.

$$= \frac{\cancel{x-3}}{(x+6)(\cancel{x-3})} , x \neq -6, 3$$

$$= \frac{1}{x+6} , x \neq -6, 3$$

c)

$$\frac{x^2 + 10x + 21}{x + 3} \quad , x \neq -3$$

$$= \frac{(x+7)\cancel{(x+3)}}{\cancel{x+3}} \quad , x \neq -3$$

$$= x + 7 \quad , x \neq -3$$

d)

$$\frac{x+1}{x^2 + 3x + 2}$$

$$= \frac{\cancel{x+1}}{(x+2)\cancel{(x+1)}} \quad , x \neq -2, -1$$

$$= \frac{1}{x+2}$$

e) $\frac{x^2 - 9}{x^2 + 7x + 12}$ ← difference of squares: $a^2 - b^2 = (a-b)(a+b)$

$$= \frac{(x-3)\cancel{(x+3)}}{(x+4)\cancel{(x+3)}} \quad ; x \neq -4, -3$$

$$= \frac{x-3}{x+4} \quad ; x \neq -4, -3$$

f) $\frac{6x^2 - 7x - 5}{3x^2 + x - 10}$

Factor numerator

$$\begin{aligned} &6x^2 - 10x + 3x - 5 \\ &= (6x^2 - 10x) + (3x - 5) \\ &= 2x(3x - 5) + 1(3x - 5) \\ &= (2x+1)(3x-5) \end{aligned}$$

Factor denominator

$$\begin{aligned} &3x^2 + x - 10 \\ &= 3x^2 + 6x - 5x - 10 \\ &= (3x^2 + 6x) + (-5x - 10) \\ &= 3x(x+2) - 5(x+2) \\ &= (x+2)(3x-5) \end{aligned}$$

$$= \frac{(2x+1)\cancel{(3x-5)}}{(x+2)\cancel{(3x-5)}} \quad ; x \neq -2, \frac{5}{3}$$

$$= \frac{2x+1}{x+2} \quad ; x \neq -2, \frac{5}{3}$$

Multiplying Rational Expressions

a)

$$\frac{2\cancel{4}x^{\cancel{2}1}}{1\cancel{3}x} \cdot \frac{4\cancel{1}2x^{\cancel{3}2}}{12x} ; x \neq 0$$

1. factor where possible
2. cancel common factors
3. multiply numerators and denominators
4. state restrictions (throughout process)

$$= 8x^3 ; x \neq 0$$

b)

$$\frac{4x+24}{x^2+8x} \cdot \frac{12x^2}{3x+18}$$

$$= \frac{4(\cancel{x+6})}{x(x+8)} \cdot \frac{4\cancel{1}2x^{\cancel{2}1}}{1\cancel{3}(x+6)} ; x \neq 0, -8, -6$$

$$= \frac{16x}{x+8} ; x \neq 0, -8, -6$$

c)

$$\frac{x+1}{2x} \cdot \frac{3x}{x^2+4x+3} \quad ; x \neq 0$$

$$= \frac{\cancel{x+1}}{2\cancel{x}} \cdot \frac{3\cancel{x}}{(\cancel{x+1})(x+3)} \quad ; x \neq 0, -1, -3$$

$$= \frac{3}{2(x+3)} \quad ; x \neq 0, -1, -3$$

d)

$$\frac{*5x^2 - 13x + 8}{x-7} \cdot \frac{1}{5x-8}$$

factor

$$\begin{aligned} &= 5x^2 - 8x - 5x + 8 \\ &= (5x^2 - 8x) + (-5x + 8) \\ &= x(5x - 8) - 1(5x - 8) \\ &= (5x - 8)(x - 1) \end{aligned}$$

$$= \frac{(\cancel{5x-8})(x-1)}{x-7} \cdot \frac{1}{\cancel{5x-8}} \quad ; x \neq 7, \frac{8}{5}$$

$$= \frac{x-1}{x-7} \quad ; x \neq 7, \frac{8}{5}$$

Dividing Rational Expressions

a)

$$\frac{10ab^2}{4a} \div \frac{15a^2}{12b^2}$$

*no cross cancelling until
after second fraction has
been flipped*

$$= \frac{10ab^2}{4a} \times \frac{12b^2}{15a^2}$$

$a \neq 0$
 $b \neq 0$

$$= \frac{\cancel{2} \cancel{12} \cancel{10} ab^4}{\cancel{60} a^3}$$

$a \neq 0$
 $b \neq 0$

$$= \frac{2b^4}{a^2}$$

$a \neq 0$
 $b \neq 0$

1. flip second fraction and change to multiplication
2. factor where possible
3. cancel common factors
4. multiply numerators and denominators
5. state restrictions (throughout process)

because 'b' was
in the denominator of
the original expression

b)

$$\frac{a^2 + 2a}{3a} \div \frac{5a^2 + 10a}{20a^2}$$

$$= \frac{a^2 + 2a}{3a} \times \frac{20a^2}{5a^2 + 10a}$$

$a \neq 0$

$$= \frac{\cancel{a}(\cancel{a+2})}{\cancel{3a}} \times \frac{\cancel{4} \cancel{20} a^2}{\cancel{5a}(\cancel{a+2})}$$

$a \neq 0, -2$

$$= \frac{4a}{3}$$

$a \neq 0, -2$

c)

$$\frac{2x^2 - 8x}{x^2 - 3x - 10} \div \frac{4x^2}{x^2 - 9x + 20}$$

$$= \frac{2x^2 - 8x}{x^2 - 3x - 10} \times \frac{x^2 - 9x + 20}{4x^2} ; x \neq 0$$

$$= \frac{\cancel{2}x \cancel{(x-4)}}{\cancel{(x-5)}(x+2)} \times \frac{\cancel{(x-5)}(x-4)}{\cancel{2}4x^2} ; x \neq 0, 5, -2, 4$$

$$= \frac{(x-4)^2}{2x(x+2)} ; x \neq 0, 5, -2, 4$$

DO WORKSHEET

2.2 Add and Subtract Rational Expressions

DO IT NOW!

$$\text{LCD} = 30$$

$$\text{a) } \frac{1 \times 6}{5 \times 6} + \frac{1 \times 6}{5 \times 6}$$

$$= \frac{6}{30} + \frac{6}{30}$$

$$= \frac{12}{30}$$

Note: the product of the denominators will give a common denominator (but not always the lowest common denominator)

b) Simplify and state restrictions

$$\frac{x^2 - 1}{x^2 - 4} \times \frac{x^2 + 3x - 4}{x^2 + 5x + 4} = \frac{(x-1)\cancel{(x+1)}}{(x-2)(x+2)} \times \frac{\cancel{(x+4)}(x-1)}{\cancel{(x+1)}\cancel{(x+1)}}$$

$$= \frac{(x-1)^2}{(x-2)(x+2)} ; x \neq 2, -2, -4, -1$$

c) $\frac{2x}{3y} + \frac{y}{6xy}$ LCD = 6xy

$$= \frac{4x^2}{6xy} + \frac{y^2}{6xy} \quad ; \begin{matrix} x \neq 0 \\ y \neq 0 \end{matrix}$$

$$= \frac{4x^2 + y^2}{6xy} \quad ; \begin{matrix} x \neq 0 \\ y \neq 0 \end{matrix}$$

Add and Subtract Rational Expressions With Monomial Denominators

a) $\frac{1}{5x} + \frac{1}{2x}$ LCD = 10x

$$\frac{2}{10x} + \frac{5}{10x}$$

$$= \frac{2}{10x} + \frac{5}{10x} \quad ; x \neq 0$$

$$= \frac{7}{10x} \quad ; x \neq 0$$

1. factor denominators if possible
2. get a common denominator
3. re-write expression with a common denominator
4. add/subtract the numerator
(keep denominator the same)
5. simplify where possible
6. state restrictions (throughout process)

b)

$$\frac{ab^2 + 2}{2ab^2} - \frac{b + 2}{2b}$$

$LCD = 2ab^2$

$$= \frac{ab^2 + 2}{2ab^2} - \frac{ab(b+2)}{2ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

$$= \frac{ab^2 + 2}{2ab^2} - \frac{ab^2 + 2ab}{2ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

$$= \frac{ab^2 + 2 - ab^2 - 2ab}{2ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

$$= \frac{2 - 2ab}{2ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

$$= \frac{\cancel{2}(1-ab)}{\cancel{2}ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

$$= \frac{1-ab}{ab^2} \quad ; \begin{matrix} a \neq 0 \\ b \neq 0 \end{matrix}$$

Add and Subtract Rational Expressions with Polynomial Denominators

a)

$LCD: (x-3)(x+2)$

1. factor denominators if possible
2. get a common denominator
3. re-write expression with a common denominator
4. add/subtract the numerator (keep denominator the same)
5. simplify where possible
6. state restrictions (throughout process)

$$\frac{(x+2)}{(x+2)} \frac{x+5}{x-3} + \frac{x-7}{x+2} \frac{(x-3)}{(x-3)}$$

$$= \frac{(x+2)(x+5)}{(x+2)(x-3)} + \frac{(x-7)(x-3)}{(x+2)(x-3)} \quad ; x \neq -2, 3$$

$$= \frac{x^2 + 7x + 10}{(x+2)(x-3)} + \frac{x^2 - 10x + 21}{(x+2)(x-3)} \quad ; x \neq -2, 3$$

$$= \frac{2x^2 - 3x + 31}{(x+2)(x-3)} \quad ; x \neq -2, 3$$

b)

$$\frac{x+9}{x^2+2x-48} - \frac{x-9}{x^2-x-30}$$

$$\text{LCD} = (x-6)(x+5)(x+8)$$

$$= \frac{\overset{(x+5)}{\cancel{(x+5)}}(x+9)}{\overset{(x+5)}{\cancel{(x+5)}}(x+8)(x-6)} - \frac{x-9}{(x-6)\overset{(x+8)}{\cancel{(x+8)}}\overset{(x+5)}{\cancel{(x+5)}}}$$

$$= \frac{(x+5)(x+9)}{(x+5)(x+8)(x-6)} - \frac{(x-9)(x+8)}{(x+5)(x+8)(x-6)}$$

$$= \frac{x^2+14x+45 - (x^2-1x-72)}{(x+5)(x+8)(x-6)}$$

$$= \frac{15x+117}{(x+5)(x+8)(x-6)} \quad ; x \neq -5, -8, 6$$

c)

$$\frac{x-2}{x+2} + \frac{x+10}{x^2+6x+8}$$

$$\text{LCD} = (x+2)(x+4)$$

$$= \frac{\overset{(x+4)}{\cancel{(x+4)}}(x-2)}{\overset{(x+4)}{\cancel{(x+4)}}(x+2)} + \frac{x+10}{(x+2)(x+4)}$$

$$= \frac{(x+4)(x-2)}{(x+4)(x+2)} + \frac{x+10}{(x+4)(x+2)}$$

$$= \frac{x^2+2x-8+x+10}{(x+4)(x+2)}$$

$$= \frac{x^2+3x+2}{(x+4)(x+2)} \quad \leftarrow \text{factor}$$

$$= \frac{\cancel{(x+2)}(x+1)}{(x+4)\cancel{(x+2)}}$$

$$= \frac{x+1}{x+4} \quad ; x \neq -4, -2$$

d)

$$\frac{2x}{x-1} - \frac{x+2}{x^2+3x-4}$$

$$\text{LCD} = (x+4)(x-1)$$

$$= \frac{(x+4)2x}{(x+4)(x-1)} - \frac{x+2}{(x+4)(x-1)}$$

$$= \frac{2x(x+4)}{(x+4)(x-1)} - \frac{x+2}{(x+4)(x-1)}$$

$$= \frac{2x^2+8x-x-2}{(x+4)(x-1)}$$

$$= \frac{2x^2+7x-2}{(x+4)(x-1)} ; x \neq -4, 1$$

e)

$$\frac{a+1}{5-2a} - \frac{a-4}{2a-5}$$

Binomial expressions can differ by a factor of -1. Factor -1 from one of the denominators to identify the common denominator. Then simplify each expression and state the restrictions.

$$= \frac{a+1}{-1(-5+2a)} - \frac{a-4}{2a-5}$$

$$= \frac{(-1)a+1}{(-1)(2a-5)} - \frac{a-4}{2a-5}$$

$$= \frac{-1(a+1)}{2a-5} - \frac{a-4}{2a-5}$$

$$= \frac{-1(a+1) - (a-4)}{2a-5}$$

$$= \frac{-a-1-a+4}{2a-5}$$

$$= \frac{-2a+3}{2a-5} ; a \neq \frac{5}{2}$$