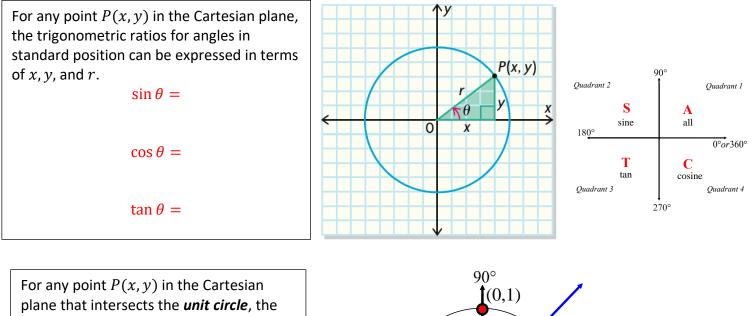
L	3 – Solving Trigonometric Equations
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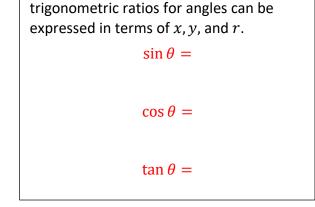
In this section, you will learn how to identify different angles that have the same trigonometric ratio, as well as learn how they are related.

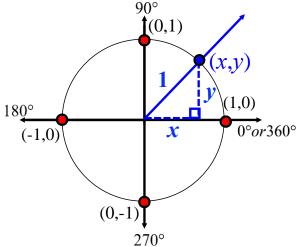
To do this you will have to visualize the terminal arm rotating around a circle centred at the origin of a grid with a radius of r. This is done so that we can extend our understanding of trig functions for a broader class of angles and see how different angles are related.

http://www.mathsisfun.com/geometry/unit-circle.html

Some helpful reminders:







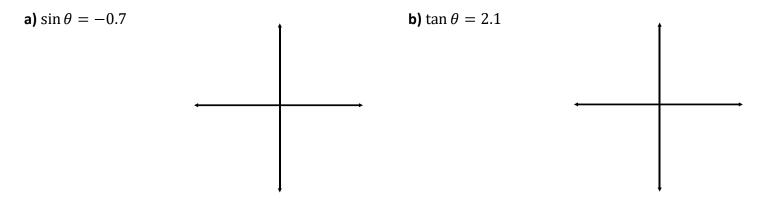
We know the x-coordinate of where the terminal arm Intersects the unit circle is equivalent to the cosine ratio and the y-coordinate is equivalent to the sine ratio.

Notice that both 45° and 135° have the same _______. Since the angles fall in quadrants _____ and _____ respectively, they will have the exact same *y*-coordinate but the *x*-coordinates will have the same absolute value but will be opposite signs.

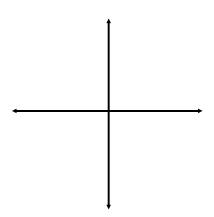
$\sin 135^\circ =$

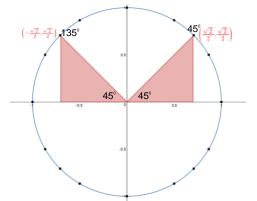
The important takeaway from this is that there are _____ between 0° and 360° that have the exact same ratio. Using reference angles and the CAST rule, we can make sure to always find both possible angles between 0° and 360° that have the same trigonometric ratio.

Example 1: Solve the following equations for $0^{\circ} \le \theta \le 360^{\circ}$. Round answers to the nearest tenth of a degree.



Example 2: The point (-7, 19) lies on the terminal arm. Find the angle to the terminal arm (principal angle, θ) and find the related acute angle (reference angle, β).





Example 3: The point P(5, 11) lies on the terminal arm of angle θ in standard position. Draw a sketch of angle θ , determine the exact value of r, determine the primary trig ratios for angle θ , then calculate θ to the nearest tenth of a degree.



Example 4: Solve the following equation for $0^{\circ} \le \theta \le 360^{\circ}$.

 $3\cos\theta + 1 = 0$

