Unit 1 - Linear Systems

1) Solve the following linear systems using substitution
a) $y=2 x-3$
$x+y=6$
b) $2 x+y=6$
$3 x+2 y=10$
c) $5=2 y-x$
$7=3 y-2 x$
d) $3 x=y+3$

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2 x+3 y=13
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e) $4 x-y=-9$
$3 y-2 x=17$
f) $4 x+y=0$
$x+2 y+1=0$
2) Solve each linear system using elimination
a) $5 x+2 y=-11$
$3 x+2 y=-9$
b) $2 x+y=-2$
$-3 x-y=3$
c) $x+y=4$
$2 x-3 y=-2$
d) $2 x-3 y=2$
$5 x+6 y=5$
e) $2 x+3 y=-2$
$8 x+5 y=-6$
f) $7 x+3 y=-17$
$6 x+2 y=-14$
g) $5 x+7 y=3$
$2 x+3 y=1$
3) Write a linear system for each question, and then solve it.
a) Three soccer balls and a basketball cost $\$ 155$. Two soccer balls and three basketballs cost $\$ 220$. Find the cost of each ball.
b) The students in the school band are selling chocolate-covered almonds for $\$ 3$ a box and chocolate bars for $\$ 2$ each to raise money for a band trip. Mary sold a total of 96 items and raised $\$ 233$. How many of each did she sell?
c) The cost of printing a magazine is based on a fixed set-up cost and the number of pages to be printed. One printing company charges a $\$ 250$ set-up fee and $\$ 5 /$ page, while a second company charges a $\$ 400$ set-up fee plus $\$ 4 /$ page. Write a linear equation for each company and then find the point of intersection. Interpret the meaning of the point of intersection.
4) Find the midpoint of each line segment
a) $A(-2,-1) B(4,3)$
e) $G(20,35) H(2,-17)$
b) $C(-4,3) D(2,-5)$
f) $A(3,-5) B(-5,-6)$
c) $A(1,7) B(9,-3)$
g) $P(-2,5) Q(6,5)$
d) $J(-3,-2) K(5,6)$
h) $A(4,1) B(-9,10)$
5. Sketch each triangle and then find the equation of the median, in slope y-intercept form, from the vertex stated:
a) Determine the equation for the median from vertex $\boldsymbol{A}$ for the triangle with vertices $A(4,4), B(-6,2)$, and $C(2,0)$
b) The vertices of $\triangle A B C$ are $A(-6,6), B(2,10)$, and $C(4,-4)$. Find the equation of the median from vertex $B$ in slope $y-$ intercept form ( $\mathrm{y}=\mathrm{mx} \mathrm{x}+\mathrm{b}$ )
c) The vertices of $\triangle P Q R$ are $P(-3,5), Q(5,7)$, and $R(3,-3)$. Find the equation of the median from vertex $Q$ in slope $y$ intercept form ( $\mathrm{y}=\mathrm{mx} \mathrm{x}+\mathrm{b}$ )
6) Find the equation of the right bisector for each of the following line segments:
a) Line Segment $A B$ : $A(-5,-2) B(3,6)$
b) Line Segment CD: $C(1,4) D(3,-2)$
c) Line Segment PQ: $\mathrm{P}(8,8) \mathrm{Q}(4,-2)$
7) Find the length of each of the following line segments (round to the nearest tenth)
a) $\mathrm{C}(-7,-5) \mathrm{D}(-4,6)$
d) $B(5,3) C(1,-5)$
b) $\mathrm{R}(-4,6) \mathrm{T}(10,-8)$

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\text { e) } S(4,-5) T(10,7)
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c) $A(-3,5) B(5,3)$
f) $\mathrm{B}(-6,8) \mathrm{C}(4,-5)$
8) Classify each of the following triangles by finding the length of each side
a) $D(-5,2), E(2,5), F(2,-1)$
b) $\mathrm{A}(-4,2), \mathrm{B}(-2,-6), \mathrm{C}(6,-2)$.
9) Determine if triangle $X(1,4) Y(-3,-2) Z(3,-6)$ is a right triangle
10) State the radius of each of the following circles
a) $x^{2}+y^{2}=49$
b) $x^{2}+y^{2}=16$
c) $x^{2}+y^{2}=64$
d) $x^{2}+y^{2}=1.44$
11) Find an equation for the circle that is centered at the origin and has:
a) radius of 4
b) a radius of $\sqrt{8}$
c) a diameter of 18
12) Find an equation for the circle centred at the origin that passes through each point.
a) $(3,-4)$
b) $(-5,2)$
c) $(3,7)$
d) $(-6,-2)$
13. Determine whether each point is on, inside, or outside the circle defined by $x^{2}+y^{2}=26$.
a) $(1,3)$
b) $(-4,6)$
c) $(1,5)$

## Answers:

1. a) $(3,3)$ b) $(2,2)$ c) $(1,3)$ d) $(2,3)$ e) $(-1,5)$ f) $(1 / 7,-4 / 7)$
2. a) $(-1,-3)$ b) $(-1,0)$ c) $(2,2)$ d) $(1,0)$ e) $(-4 / 7,-2 / 7)$ f) $(-2,-1)$ g) $(2,-1)$
3. a) soccer $=35$, bball $=50$ b) 41 almonds, 55 choc. Bars c) same cost of 1000 when printing 150 pgs
4. a) $(1,1)$ b) $(-1,-1)$ c) $(5,2)$ d) $(1,2)$ e) $(11,9)$ f) $(-1,-11 / 2)$ g) $(2,5)$ h) $(-5 / 2,11 / 2)$
$\begin{array}{lll}\text { 5. a) } y=1 / 2 x+2 & \text { b) } 3 x+4 & \text { c) } 6 / 5 x+1\end{array}$
5. a) $y=-x+1$ b) $1 / 3 x+1 / 3$ c) $y=-2 / 5 x+27 / 5$
6. a) 11.4 b) 19.8 c) 8.2 d) 8.9 e) 13.4 f) 16.4
7. a) isosceles b) scalene
8. yes it is a right triangle
9. a) 7 b) 4 c) 8 d) 1.2
10. a) $x^{2}+y^{2}=16$ b) $x^{2}+y^{2}=8$ c) $x^{2}+y^{2}=81$
11. a) $x^{2}+y^{2}=25$ b) $x^{2}+y^{2}=29$ c) $x^{2}+y^{2}=58$ d) $x^{2}+y^{2}=40$
12. a) inside b) outside c) on
