

1.4 Working with Radicals - Worksheet

MCR3U

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SOLUTIONS

1) Simplify

a) $3(4\sqrt{5})$

= $12\sqrt{5}$

b) $\sqrt{5}(-2\sqrt{7})$

= $-2\sqrt{35}$

c) $2\sqrt{3}(3\sqrt{2})$

= $6\sqrt{6}$

2) Express each as a mixed radical in simplest form

a) $\sqrt{12}$

= $\sqrt{4} \times \sqrt{3}$

= $2\sqrt{3}$

b) $\sqrt{147}$

= $\sqrt{49 \times 3}$

= $\sqrt{49} \times \sqrt{3}$

= $7\sqrt{3}$

c) $\sqrt{252}$

= $\sqrt{36 \times 7}$

= $\sqrt{36} \times \sqrt{7}$

= $6\sqrt{7}$

3) Simplify

a) $2\sqrt{3} - 5\sqrt{3} + 4\sqrt{3}$

= $1\sqrt{3}$

b) $11\sqrt{5} - 4\sqrt{5} - 5\sqrt{5} - 6\sqrt{5}$

= $-4\sqrt{5}$

c) $\sqrt{6} - 4\sqrt{2} + 3\sqrt{6} - \sqrt{2}$

= $4\sqrt{6} - 5\sqrt{2}$

d) $2\sqrt{10} - \sqrt{10} - 4\sqrt{10} + \sqrt{5}$

= $-3\sqrt{10} + \sqrt{5}$

4) Add or subtract as indicated

a) $8\sqrt{2} - 4\sqrt{8} + \sqrt{32}$

= $8\sqrt{2} - 4(\sqrt{4}\sqrt{2}) + (\sqrt{16})(\sqrt{2})$

b) $\sqrt{20} - 4\sqrt{12} - \sqrt{125} + 2\sqrt{3}$

= $(\sqrt{4}\sqrt{5}) - 4(\sqrt{4}\sqrt{3}) - (\sqrt{25}\sqrt{5}) + 2\sqrt{3}$

= $2\sqrt{5} - 8\sqrt{3} - 5\sqrt{5} + 2\sqrt{3}$

= $-3\sqrt{5} - 6\sqrt{3}$

= $4\sqrt{2}$

c) $5\sqrt{3} - \sqrt{72} + \sqrt{243} + \sqrt{8}$

$$\begin{aligned}&= 5\sqrt{3} \cdot (\sqrt{3})(\sqrt{2}) + (\sqrt{8})(\sqrt{3}) + (\sqrt{4})(\sqrt{2}) \\&= 5\sqrt{3} \cdot (6\sqrt{2} + 9\sqrt{3} + 2\sqrt{2}) \\&= 14\sqrt{3} - 4\sqrt{2}\end{aligned}$$

d) $\sqrt{44} + \sqrt{88} + \sqrt{99} + \sqrt{198}$

$$\begin{aligned}&= (\sqrt{4})(\sqrt{11}) + (\sqrt{4})(\sqrt{22}) + (\sqrt{9})(\sqrt{11}) + (\sqrt{9})(\sqrt{22}) \\&= 2\sqrt{11} + 2\sqrt{22} + 3\sqrt{11} + 3\sqrt{22} \\&= 5\sqrt{11} + 5\sqrt{22}\end{aligned}$$

5) Expand and simplify

a) $5\sqrt{6}(2\sqrt{3})$

$$\begin{aligned}&= 10\sqrt{18} \\&= 10(\sqrt{9})(\sqrt{2}) \\&= 30\sqrt{2}\end{aligned}$$

b) $8\sqrt{5}(\sqrt{10})$

$$\begin{aligned}&= 8\sqrt{50} \\&= 8(\sqrt{25})(\sqrt{2}) \\&= 40\sqrt{2}\end{aligned}$$

c) $11\sqrt{2}(5\sqrt{3})$

$$= 55\sqrt{6}$$

6) Expand and simplify where possible

a) $3(8 - \sqrt{5})$

$$= 24 - 3\sqrt{5}$$

b) $\sqrt{3}(\sqrt{6} - \sqrt{3})$

$$\begin{aligned}&= \sqrt{18} - \sqrt{9} \\&= (\sqrt{9})(\sqrt{2}) - \sqrt{9} \\&= 3\sqrt{2} - 3\end{aligned}$$

c) $8\sqrt{2}(2\sqrt{8} + 3\sqrt{12})$

$$\begin{aligned}&= 16\sqrt{16} + 24\sqrt{24} \\&= 64 + 24(\sqrt{4})(\sqrt{6}) \\&= 64 + 48\sqrt{6}\end{aligned}$$

7) Expand and simplify where possible

a) $(\sqrt{2} + 5)(\sqrt{2} + 5)$

$$\begin{aligned}&= \cancel{\sqrt{4}} + 5\sqrt{2} + 5\sqrt{2} + 25 \\&= 2 + 10\sqrt{2} + 25 \\&= 27 + 10\sqrt{2}\end{aligned}$$

b) $(\sqrt{3} + 2\sqrt{2})(5 + 5\sqrt{2})$

$$\begin{aligned}&= 5\sqrt{3} + 5\sqrt{6} + 10\sqrt{2} + 10\sqrt{4} \\&= 5\sqrt{3} + 5\sqrt{6} + 10\sqrt{2} + 20\end{aligned}$$

c) $(1 + \sqrt{5})(1 - \sqrt{5})$ D.O.S.

$$\begin{aligned}&= (1)^2 - (\sqrt{5})^2 \\&= 1 - 5 \\&= -4\end{aligned}$$

d) $(4 - 3\sqrt{7})(\sqrt{7} + 1)$

$$\begin{aligned}&= 4\sqrt{7} + 4 - 3\sqrt{49} - 3\sqrt{7} \\&= 1\cancel{\sqrt{7}} + 4 - 21 \\&= \cancel{\sqrt{7}} - 17\end{aligned}$$

8) Simplify

a) $\frac{1}{4}\sqrt{54} - \frac{1}{4}\sqrt{150}$

$$= \frac{1}{4}(\sqrt{4})(\sqrt{6}) - \frac{1}{4}(\sqrt{25})(\sqrt{6})$$

$$= \frac{3}{4}\sqrt{6} - \frac{5}{4}\sqrt{6}$$

$$= -\frac{1}{2}\sqrt{6}$$

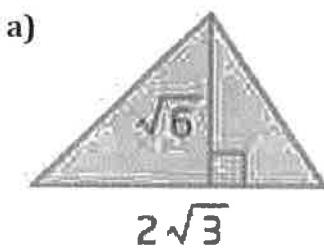
b) $\frac{1}{2}\sqrt{8} + \frac{3}{5}\sqrt{50} - \frac{2}{3}\sqrt{18}$

$$= \frac{1}{2}(\sqrt{4})(\sqrt{2}) + \frac{3}{5}(\sqrt{25})(\sqrt{2}) - \frac{2}{3}(\sqrt{9})(\sqrt{2})$$

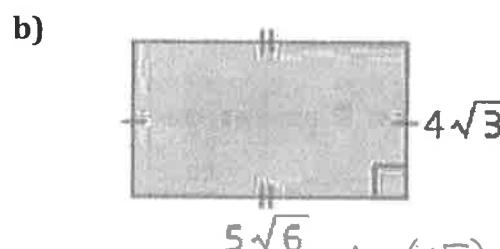
$$= 1\sqrt{2} + 3\sqrt{2} - 2\sqrt{2}$$

$$= 2\sqrt{2}$$

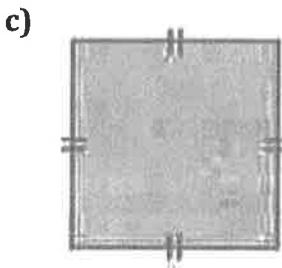
9) Find a simplified expression for the area of each shape



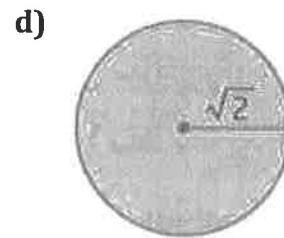
$$\begin{aligned} A &= \frac{\sqrt{3}(\sqrt{6})}{2} \\ &= \sqrt{18} \\ &= (\sqrt{9})(\sqrt{2}) \\ &= 3\sqrt{2} \end{aligned}$$



$$\begin{aligned} A &= (5\sqrt{6})(4\sqrt{3}) \\ &= 20\sqrt{18} \\ &= 20(\sqrt{9})(\sqrt{2}) \\ &= 60\sqrt{2} \end{aligned}$$

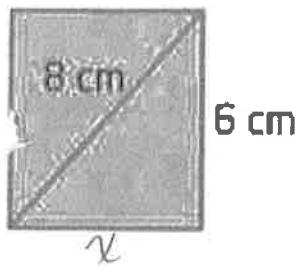


$$\begin{aligned} A &= (3\sqrt{5})^2 \\ &= 9(5) \\ &= 45 \end{aligned}$$



$$\begin{aligned} A &= \pi(\sqrt{2})^2 \\ &= 2\pi \end{aligned}$$

10) Find the area and perimeter of the rectangle shown. Express your answer in simplified radical form.



$$x^2 + 6^2 = 8^2$$

$$x^2 = 64 - 36$$

$$x = \sqrt{28}$$

$$x = 2\sqrt{7}$$

$$A = (2\sqrt{7})(6)$$

$$= 12\sqrt{7} \text{ cm}^2$$

$$P = 2(2\sqrt{7}) + 2(6)$$

$$= 4\sqrt{7} + 12 \text{ cm}$$

11) Simplify each of the following

a) $\frac{21-7\sqrt{6}}{7}$

$$= \frac{7(3-\sqrt{6})}{7}$$

$$= 3 - \sqrt{6}$$

b) $\frac{12-\sqrt{48}}{4}$

$$= \frac{12 - (\sqrt{16})(\sqrt{3})}{4}$$

$$= \frac{12 - 4\sqrt{3}}{4}$$

$$= \frac{4(3-\sqrt{3})}{4}$$

$$= 3 - \sqrt{3}$$

Answers

1) a) $12\sqrt{5}$ b) $-2\sqrt{35}$ c) $6\sqrt{6}$

2) a) $2\sqrt{3}$ b) $7\sqrt{3}$ c) $6\sqrt{7}$

3) a) $\sqrt{3}$ b) $-4\sqrt{5}$ c) $4\sqrt{6} - 5\sqrt{2}$ d) $-3\sqrt{10} + \sqrt{5}$

4) a) $4\sqrt{2}$ b) $-3\sqrt{5} - 6\sqrt{3}$ c) $14\sqrt{3} - 4\sqrt{2}$ d) $5\sqrt{11} + 5\sqrt{22}$

5) a) $30\sqrt{2}$ b) $40\sqrt{2}$ c) $55\sqrt{6}$

6) a) $24 - 3\sqrt{5}$ b) $3\sqrt{2} - 3$ c) $64 + 48\sqrt{6}$

7) a) $27 + 10\sqrt{2}$ b) $5\sqrt{3} + 5\sqrt{6} + 10\sqrt{2} + 20$ c) -4 d) $-17 + \sqrt{7}$

8) a) $-\frac{1}{2}\sqrt{6}$ b) $2\sqrt{2}$

9) a) $3\sqrt{2}$ b) $60\sqrt{2}$ c) 45 d) 2π

10) area = $12\sqrt{7}$ cm²; perimeter = $12 + 4\sqrt{7}$ cm

11) a) $3 - \sqrt{6}$ b) $3 - \sqrt{3}$