## W2 – Solving Linear Systems by SUBSTITUTION

MPM2D

Jensen

1) Solve each linear system using the method of substitution. Check your answers.

a) 
$$\ell_1: y = 3x - 4$$
  
 $\ell_2: x + y = 8$ 

**b)** 
$$\ell_1: x = -4y + 5$$
  $\ell_2: x + 2y = 7$ 

c) 
$$\ell_1: y = -2x + 3$$
  
 $\ell_2: 4x - 3y = 1$ 

d) 
$$\ell_1: 2x + 4y = 2$$
  
 $\ell_2: x = 1 - 2y$ 

e) 
$$\ell_1: x + 2y = 3$$
  
 $\ell_2: 5x + 4y = 8$ 

f) 
$$\ell_1: 6x + 5y = 7$$
  
 $\ell_2: x - y = 3$ 

g) 
$$\ell_1: 2m + n = 2$$
  
 $\ell_2: 3m - 2n = 3$ 

h) 
$$\ell_1: 3a + 2b = 4$$
  
 $\ell_2: 2a + b = 6$ 

i) 
$$\ell_1: 2x + y = 4$$
  
 $\ell_2: 4x - y = 2$ 

2) Find the point of intersection of each pair of lines.

a) 
$$\ell_1$$
:  $2x = y + 5$   
 $\ell_2$ :  $3x + y = -9$ 

b) 
$$\ell_1: 4x + 2y = 7$$
  
 $\ell_2: -x - 7y = 6$ 

c) 
$$\ell_1: p + 4q = 3$$
  
 $\ell_2: 5p = -2q + 3$ 

d) 
$$\ell_1: a+b+6=0$$
  
 $\ell_2: 2a-b-3=0$ 

e) 
$$\ell_1: x - 2y - 2 = 0$$
  
 $\ell_2: 3x + 4y - 16 = 0$ 

- **3)** Samantha works twice as many hours per week as Adriana. Together they work a total of 39 hours in one week.
- a) Write an equation to represent the information in the first sentence.
- **b)** Write an equation to represent the information in the second sentence.

c) Use the method of substitution to find the number of hours worked by each person.
<b>4)</b> Ugo plays hockey and is awarded 2 points for each goal and 1 point for each assist. Last season he had a total of 86 points. He scored 17 fewer goals than assists.
a) Write a linear system to represent the information
b) Solve the system
c) What does the solution represent in the context of this question?
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- **5)** Joanne's family decides to rent a hall for her retirement party. Pin Hall charges \$500 for the hall and \$15 per meal. Bloom Place charges \$350 for the hall and \$18 per meal.
- a) Write two equations to represent the information.
- b) Solve the linear system to find the number of guests for which the charges are the same at both halls.

## **Answers:**

**1) a)** 
$$x = 3, y = 5$$
 **b)**  $x = 9, y = -1$  **c)**  $x = 1, y = 1$  **d)** infinite solutions

e) 
$$x = \frac{2}{3}$$
,  $y = \frac{7}{6}$  f)  $x = 2$ ,  $y = -1$  g)  $m = 1$ ,  $n = 0$  h)  $a = 8$ ,  $b = -10$  i)  $x = 1$ ,  $y = 2$ 

2)a) 
$$x = -\frac{4}{5}$$
,  $y = -\frac{33}{5}$  b)  $x = \frac{61}{26}$ ,  $y = -\frac{31}{26}$  c)  $p = \frac{1}{3}$ ,  $q = \frac{2}{3}$  d)  $a = -1$ ,  $b = -5$  e)  $x = 4$ ,  $y = 1$ 

3)a) 
$$S=2a$$
 b)  $S+A=39$  c) Samantha worked 26 hours and Adriana worked 13 hours

**4)a)** 
$$2g + a = 86$$
;  $g = a - 17$  **b)**  $g = 23$ ,  $a = 40$  **c)** 23 goals; 40 assists

**5)a)** 
$$C = 500 + 15n$$
;  $C = 350 + 18n$  **b)** 50 guests