

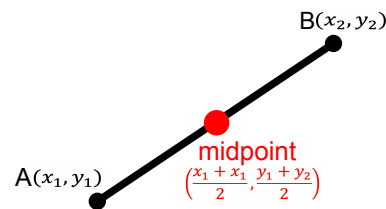
## L1 – Midpoint and Length of a Line Segment

Unit 2

MPM2D

Jensen

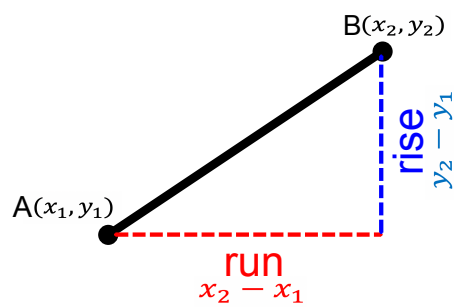
To find the                      of a line segment, you must find the middle (average) of both the  $x$  and  $y$  coordinates of the endpoints. If A has coordinates  $(x_1, y_1)$  and B has coordinates  $(x_2, y_2)$ , then the coordinates of the midpoint of line segment AB are  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$



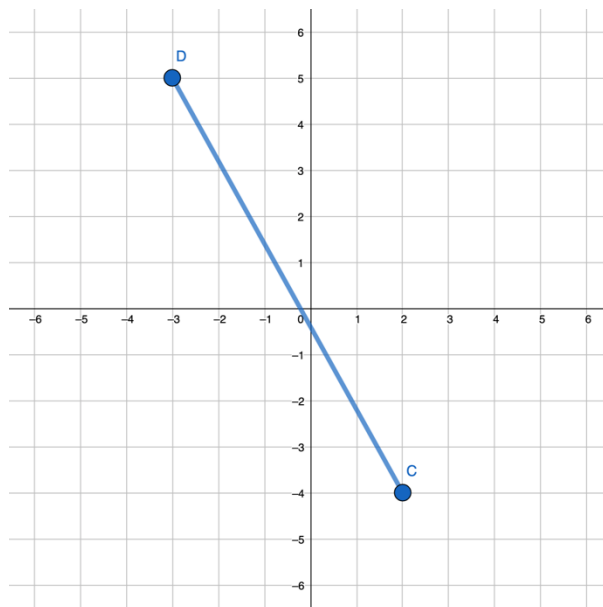
To find the                      of a line segment, we first construct a right-angle triangle using the rise and run of the line segment. The run is the difference in the  $x$ -coordinates of the endpoints, and the rise is the difference in the  $y$ -coordinates of the endpoints. You can then use Pythagorean Theorem,  $a^2 + b^2 = c^2$  to calculate the length of the line segment.

$$(\text{length of } AB)^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2$$

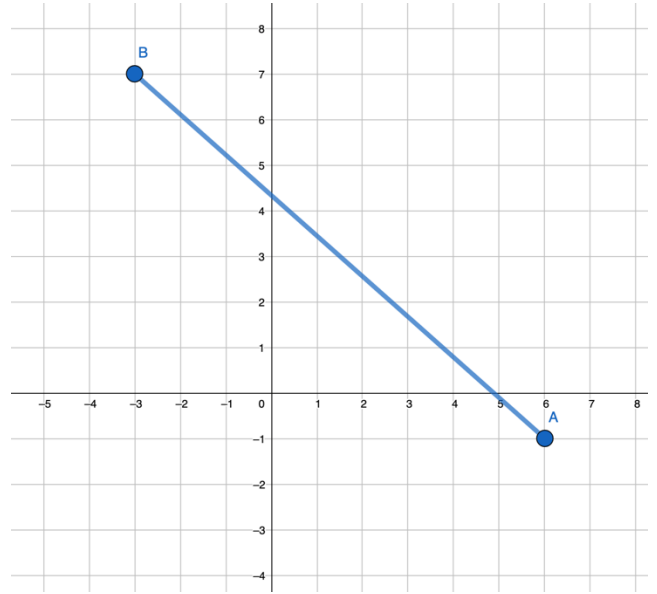
$$\text{length of } AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



**Example 1:** Calculate the length and midpoint of the line segment joining the endpoints C(2, -4) and D(-3, 5).



**Example 2:** Calculate the length and midpoint of the line segment joining the endpoints  $A(6, -1)$  and  $B(-3, 7)$ .

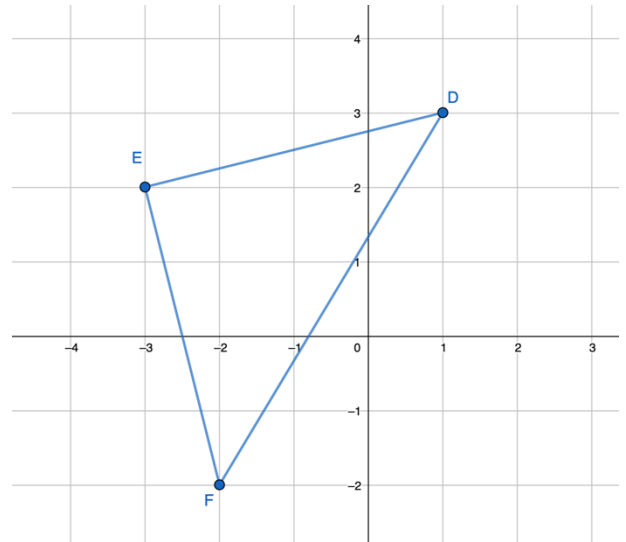


**Example 3:** Calculate the length and midpoint of the line segment joining the endpoints  $E\left(-\frac{5}{8}, \frac{1}{8}\right)$  and  $F\left(4, \frac{3}{4}\right)$ .

**Example 4:** If line segment AB has point  $A(5, 7)$  and a midpoint at  $(4, 8)$ , what are the coordinates of point B?

**Example 5:** Triangle DEF has vertices  $D(1,3)$ ,  $E(-3,2)$ , and  $F(-2,-2)$ .

**a)** Classify the triangle by side length



**b)** Determine the perimeter of the triangle rounded to the nearest tenth.

**c)** Is it a right-angle triangle? Give proof.