

W3 – Factor $x^2 + bx + c$

Unit 3

MPM2D

Jensen

1) Factor, if possible.

a) $x^2 + 7x + 10$

$$\begin{array}{r} \underline{2} \times \underline{5} = 10 \\ \underline{2} + \underline{5} = 7 \end{array}$$

$$= (x+2)(x+5)$$

b) $j^2 + 12j + 27$

$$\begin{array}{r} \underline{9} \times \underline{3} = 27 \\ \underline{9} + \underline{3} = 12 \end{array}$$

$$= (j+9)(j+3)$$

c) $k^2 + 5k + 4$

$$\begin{array}{r} \underline{4} \times \underline{1} = 4 \\ \underline{4} + \underline{1} = 5 \end{array}$$

$$= (k+4)(k+1)$$

d) $p^2 + 9p + 12$

$$\begin{array}{r} \underline{\quad} \times \underline{\quad} = 12 \\ \underline{\quad} + \underline{\quad} = 9 \end{array}$$

not factorable

e) $w^2 + 11w + 25$

$$\begin{array}{r} \underline{\quad} \times \underline{\quad} = 25 \\ \underline{\quad} + \underline{\quad} = 11 \end{array}$$

not factorable

f) $d^2 + 10d + 24$

$$\begin{array}{r} \underline{6} \times \underline{4} = 24 \\ \underline{6} + \underline{4} = 10 \end{array}$$

$$= (d+6)(d+4)$$

2) Factor, if possible.

a) $m^2 - 7m + 10$

$$\begin{array}{r} \underline{-2} \times \underline{-5} = 10 \\ \underline{-2} + \underline{-5} = -7 \end{array}$$

$$= (m-2)(m-5)$$

b) $x^2 - 5x + 7$

$$\begin{array}{r} \underline{\quad} \times \underline{\quad} = 7 \\ \underline{\quad} + \underline{\quad} = -5 \end{array}$$

not factorable

c) $y^2 - 5y + 4$

$$\begin{array}{r} \underline{-4} \times \underline{-1} = 4 \\ \underline{-4} + \underline{-1} = -5 \end{array}$$

$$= (y-4)(y-1)$$

d) $r^2 - 16r + 64$

$$\begin{array}{r} \underline{-8} \times \underline{-8} = 64 \\ \underline{-8} + \underline{-8} = -16 \end{array}$$

$$= (r-8)(r-8)$$

$$= (r-8)^2$$

e) $w^2 - 9w + 24$

$$\begin{array}{r} \underline{\quad} \times \underline{\quad} = 24 \\ \underline{\quad} + \underline{\quad} = -9 \end{array}$$

NOT factorable

f) $q^2 - 10q + 9$

$$\begin{array}{r} \underline{-9} \times \underline{-1} = 9 \\ \underline{-9} + \underline{-1} = -10 \end{array}$$

$$= (q-9)(q-1)$$

3) Factor, if possible.

a) $a^2 - 3a - 10$

$$\begin{array}{r} \underline{-5} \times \underline{2} = -10 \\ \underline{-5} + \underline{2} = -3 \end{array}$$

$$= (a-5)(a+2)$$

b) $s^2 + 3s - 10$

$$\begin{array}{r} \underline{5} \times \underline{-2} = -10 \\ \underline{5} + \underline{-2} = 3 \end{array}$$

$$= (s+5)(s-2)$$

c) $d^2 - 8d - 9$

$$\begin{array}{r} \underline{-9} \times \underline{1} = -9 \\ \underline{-9} + \underline{1} = -8 \end{array}$$

$$= (d-9)(d+1)$$

d) $f^2 + 7f - 6$

$\underline{\quad} \times \underline{\quad} = -6$
$\underline{\quad} + \underline{\quad} = 7$

not factorable

e) $g^2 - 5g - 14$

$\underline{-7} \times \underline{2} = -14$
$\underline{-7} + \underline{2} = -5$

$$= (g-7)(g+2)$$

f) $r^2 + 2r - 6$

$\underline{\quad} \times \underline{\quad} = -6$
$\underline{\quad} + \underline{\quad} = 2$

not factorable

g) $x^2 + x - 42$

$\underline{7} \times \underline{-6} = -42$
$\underline{7} + \underline{-6} = 1$

$$= (x+7)(x-6)$$

h) $b^2 - 2b - 4$

$\underline{\quad} \times \underline{\quad} = -4$
$\underline{\quad} + \underline{\quad} = -2$

not factorable

i) $x^2 + xy - 42y^2$

$\underline{7} \times \underline{-6} = -42$
$\underline{7} + \underline{-6} = 1$

$$= (x+7y)(x-6y)$$

j) $x^2 - 8xy - 48y^2$

$\underline{-12} \times \underline{4} = -48$
$\underline{-12} + \underline{4} = -8$

$$= (x - 12y)(x + 4y)$$

k) $x^4 + 11x^2 + 24$

Let $k = x^2$

$$= k^2 + 11k + 24$$

$$= (k+8)(k+3)$$

$$= (x^2+8)(x^2+3)$$

$\underline{8} \times \underline{3} = 24$
$\underline{8} + \underline{3} = 11$

l) $x^2 - 9$

$\underline{3} \times \underline{-3} = -9$
$\underline{3} + \underline{-3} = 0$

$$= (x+3)(x-3)$$

4) Factor, if possible.

a) $3x^2 + 12x + 9$

$$= 3(x^2 + 4x + 3)$$

$$\approx 3(x+3)(x+1)$$

$\underline{3} \times \underline{1} = 3$
$\underline{3} + \underline{1} = 4$

b) $2d^2 - 22d + 56$

$$= 2(d^2 - 11d + 28)$$

$$= 2(d-7)(d-4)$$

$\underline{-7} \times \underline{-4} = 28$
$\underline{-7} + \underline{-4} = -11$

c) $5z^2 + 40z + 60$

$$= 5(z^2 + 8z + 12)$$

$$= 5(z+2)(z+6)$$

$\underline{2} \times \underline{6} = 12$
$\underline{2} + \underline{6} = 8$

d) $4s^2 - 8s - 32$

$$= 4(s^2 - 2s - 8)$$

$$= 4(s-4)(s+2)$$

$\underline{\quad} \times \underline{\quad} =$
$\underline{\quad} + \underline{\quad} =$

5) Factor, if possible.

a) $x^4 + 10x^2y + 9y^2$

Let $k = x^2$

$$\begin{aligned} &= k^2 + 10ky + 9y^2 \\ &= (k+9y)(k+y) \\ &= (x^2+9y)(x^2+y) \end{aligned}$$

$$\begin{array}{rcl} \frac{9}{9} \times \frac{1}{1} &=& 9 \\ \hline \frac{9}{9} + \frac{1}{1} &=& 10 \end{array}$$

b) $(x+a)^2 + 3(x+a) + 2$

Let $k = x+a$

$$\begin{aligned} &= k^2 + 3k + 2 \\ &= (k+2)(k+1) \\ &= (x+a+2)(x+a+1) \end{aligned}$$

$$\begin{array}{rcl} \frac{2}{2} \times \frac{1}{1} &=& 2 \\ \hline \frac{2}{2} + \frac{1}{1} &=& 3 \end{array}$$

6) Determine binomials that represent the length and width of the rectangle. Then, determine the dimensions of the rectangle if x represents 15 cm.

$$\begin{aligned} A &= x^2 + 18x + 80 \\ A &= (\underline{x+10})(\underline{x+8}) \\ &\quad \text{length} \quad \text{width} \end{aligned}$$

$$\begin{array}{rcl} \frac{10}{10} \times \frac{8}{8} &=& 80 \\ \hline \frac{10}{10} + \frac{8}{8} &=& 18 \end{array}$$

Area is
 $x^2 + 18x + 80$

A = (15+10)(15+8)

A = (25)(23)

A = 575 cm²

The length is 25 cm
 The width is 23 cm

Answers

- 1)a) $(x+5)(x+2)$ b) $(j+9)(j+3)$ c) $(k+4)(k+1)$ d) not possible e) not possible f) $(d+6)(d+4)$
 2)a) $(m-2)(m-5)$ b) not possible c) $(y-4)(y-1)$ d) $(r-8)^2$ e) not possible f) $(q-9)(q-1)$
 3)a) $(a-5)(a+2)$ b) $(s+5)(s-2)$ c) $(d-9)(d+1)$ d) not possible e) $(g-7)(g+2)$ f) not possible
 g) $(x+7)(x-6)$ h) not possible i) $(x+7y)(x-6y)$ j) $(x-12y)(x+4y)$ k) $(x^2+8)(x^2+3)$ l) $(x-3)(x+3)$
 4)a) $3(x+3)(x+1)$ b) $2(d-7)(d-4)$ c) $5(z+6)(z+2)$ d) $4(s-4)(s+2)$
 5)a) $(x^2+9y)(x^2+y)$ b) $(x+a+2)(x+a+1)$
 6) A = $(x+10)(x+8)$; the rectangle is 25 cm by 23 cm.