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<mark>L6 – 2.5 – Solving Inequalities Lesson</mark>
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In this section, you will learn the meaning of a polynomial inequality and examine methods for solving polynomial inequalities.

Part 1: Intro to Inequalities

Task: Read the following on your own

Examine the graph of $y = x^2 + 4x - 12$.

The *x*-intercepts are 6 and -2. These correspond to the zeros of the function $y = x^2 + 4x - 12$. Note that the factored form version of the function is y = (x + 6)(x - 2). By moving from left to right along the *x*-axis, we can make the following observations:

- The function is positive when *x* < −6 since the *y*-values are positive
- The function is negative when -6 < x < 2 since the *y*-values are negative
- The function is positive when *x* > 2 since the *y*-values are positive.



The zeros -6 and 2 divide the *x*-axis into three intervals. In each interval, the function is either positive or negative. The information can be summarized in a table:

Interval	<i>x</i> < -6	-6 < x < 2	<i>x</i> > 2
Sign of Function	+	—	+



Polynomial Inequalities

A polynomial inequality results when the equal sign in a polynomial equation is replaced with an inequality symbol.

The real zeros of a polynomial function, or *x*-intercepts of the corresponding graph, divide the *x*-axis into intervals that can be used to solve a polynomial inequality.

Part 1: Inequalities and Number Lines

Example 1: Write an inequality that corresponds to the values of *x* shown on each number line



Part 2: Solve an Inequality given the Graph

Example 2: Use the graph of the function f(x) to answer the following inequalities...



Part 2: Solve Linear Inequalities

Note: Solving linear _______ is the same as solving linear ______. However, when both sides of an inequality are multiplied or divided by a ______ number, the inequality sign must be

Example 3: Solve each inequality **a)** $x - 8 \ge 3$

b) −4 − 2*x* < 12

Part 2: Solve Inequalities of Degree 2 and Higher

Steps for solving polynomial inequalities algebraically:

- 1) Use inverse operations to move all terms to one side of the inequality
- 2) Factor the polynomial to determine the zeros of the corresponding equation
- **3)** Find the interval(s) where the function is positive or negative by either:
 - **a.** Graphing the function using the zeros, leading coefficient, and degree
 - **b.** Make a factor table and test values in each interval

Example 4: Solve each polynomial inequality algebraically

a) $2x^2 + 3x - 9 > 0$

Method 1: Graph the inequality



To make a factor table:

- Use *x*-intercepts and vertical asymptotes to divide in to intervals
- Use a test point within each interval to find the sign of each factor
- Determine the overall sign of the product by multiplying signs of each factor within each interval.

b) $-2x^3 - 6x^2 + 12x \le -16$

Method 1: Graph the inequality



Method 2: Factor Table (sign chart)

Part 2: Applications of Inequalities

3) The price, *p*, in dollars, of a stock *t* years after 1999 can be modeled by the function $p(t) = 0.5t^3 - 5.5t^2 + 14t$. When will the price of the stock be more than \$90?