3.3 Discover the Exponent Laws

DO IT NOW

I have a bag containing 24 coloured marbles. The colours are red, green and blue. There are twice as many red marbles as green marbles, and one more red marble than blue marble. How many of each colour marble are there?

Red: 10 Green: 5 Blue: 9

Part 1: Exponent Laws Investigation

Product Rule: Complete the following table

Product	Expanded Form	Single Power
3 ² · 3 ⁴	(3 x 3) x (3 x 3 x 3 x 3) = 3 x 3 x 3 x 3 x 3 x 3	3 ⁶
43.43	(4x4x4) x (4x4x4) = 4x4x4x4x4x4x4	46
23 · 24 · 22	= 3x3x3 x3x3x3x3x3x3 (3x3x3)x(3x3x3x3)x(3x9)	a ⁹
k ³ · k ⁵	(KxKxK)x(kxkxkxkxk) =kxkxkxkxkxkxkxk	۲ ⁸
create your own example		

Describe any trends you see:

When multiplying powers with the same base, keep the base the same and add the exponents.

Quotient Rule: Complete the following table

Quotient	Expanded Form	Single Power
5 ⁵ ÷ 5 ³	_5x5x&x&x& 8x8x8	52
7 ⁴ ÷ 7 ¹	<u>אראראר /</u>	7 ³
10 ⁶ ÷ 10 ⁴	YQX QX A YQX O YQY O YQY O YQY O YQY O YQY YQY YQY Y	10ª
$x^8 \div x^5$	(12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22)(22) (12)(22)(22)(22) (12)(22)(22)(22) (12)(22)(22)(22) (12)(22)(22) (12)(22)(22) (12)(22)(22) (12)(22)(22) (12)(22)	χ ³
create your own example		

Describe any trends you see:

When dividing powers with the same base, keep the base the same and subtract the exponents.

Power of a Power Rule: Complete the following table

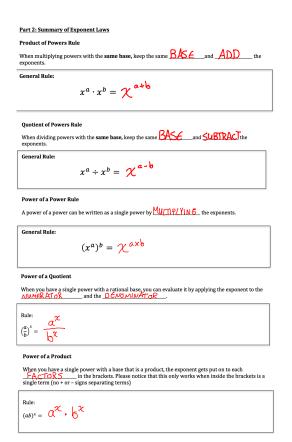
Power of a Power	Expanded Form	Single Power
$(2^2)^3$	$(2^2) \times (2^2) \times (2^2)$ = $(2 \times 2) \times (2 \times 2) \times (2 \times 2)$ = $2 \times 2 \times 2 \times 2 \times 2 \times 2$	2 ⁶
(5 ³) ⁴	(5 ³)x(5 ³)x(5 ³)x(5 ³) =(5x5x5)x(5x5x5)x(5x5x6)x(5x5x5) = 5x5x5x5x5x5x5x5x6x5x5x5x5x5x5	5 ^k
$(10^4)^2$	(וו ⁴) א (ומ ⁴) > (א או א אוא או אוא אוא אוא אוא אוא אוא	IO ₈
Create your own example		

Describe any trends you see:

A power of a power can be written as a single power by keeping the base the same and multiplying the exponents.

Summary of Exponent Laws:

Product Rule	$x^a \cdot x^b = \chi^{a+b}$
Quoutient Rule	$x^{a} \div x^{b} = \chi^{a-b}$
Power of a Power Rule	$(x^a)^b = \chi^{a \times b}$
Zero Exponent Rule	$x^0 = 1$



Part 3: Apply the Product Rule

$$x^{a} \cdot x^{b} = x^{a+b}$$

Write each product as a single power. Then, evaluate the power where possible.

1)
$$3^2 \times 3^3$$

= 3^{8+3}
= 3^5
= 2^{1}
= 3^5
= 3^5
= 3^5
= 3^5
= 3^5
= 3^5
= 3^5

3)
$$(x^{2})(x^{7})$$

= χ^{2+7}
= χ^{9}
2) $(a^{4})(a^{4})(a^{5})$
= α^{4+4+5}
= α^{13}

5)
$$(-2)^4 \times (-2)^3$$

= $(-2)^{4+3}$
= $(-2)^7$
= -128

6)
$$\left(\frac{1}{2}\right)^3 \times \left(\frac{1}{2}\right)^2$$

$$= \left(\frac{1}{2}\right)^{3+2}$$

$$= \left(\frac{1}{2}\right)^5$$

$$= \frac{1^5}{2^5}$$

$$= \frac{1}{32}$$

Part 4: Apply the Quotient Rule

$$x^{a} \div x^{b} = x^{a-b}$$

Write each quotient as a single power. Then, evaluate the power where possible.

7)
$$8^7 \div 8^5$$
= 8^{7-5}
= 8^2
= 64

8)
$$4^7 \div 4 \div 4^3$$

= 4^{7-1-3}
= 4^3
= 64

9)
$$x^{70} \div x^{40} \div x^{29}$$

= $\chi^{70-40-29}$
= χ^{1}
= χ^{1}

$$10) \frac{x^7}{x^3}$$

$$= \chi^{7-3}$$

$$= \chi^4$$

11)
$$\frac{(-0.5)^6}{(-0.5)^3}$$

12)
$$\frac{\left(\frac{3}{4}\right)^3 \times \left(\frac{3}{4}\right)^2}{\left(\frac{3}{4}\right)^5}$$

$$=\frac{\left(\frac{3}{4}\right)^5}{\left(\frac{3}{4}\right)^5}$$

$$= \left(\frac{3}{4}\right)^{5-5}$$

$$=\left(\frac{3}{4}\right)^0$$

13)
$$\frac{a^5a^2}{a^6a^1}$$

$$= \frac{Q^{S+2}}{Q^{6+1}}$$

$$=\frac{a^7}{a^7}$$

$$= a^{7-7}$$

Part 5: Apply the Power of a Power Rule

$$(x^a)^b = x^{a \times b}$$

Write each power of a power as a single power. Then, evaluate the power where possible.

14)
$$(3^2)^4$$

$$=3^{2x4}$$

15)
$$[(-2)^3]^4$$

$$16) \left[\left(\frac{2}{3} \right)^2 \right]^2$$

$$=\left(\frac{3}{3}\right)^{2\times 3}$$

$$=\left(\frac{2}{3}\right)^{4}$$

$$=(-2)^3x^4$$

$$= (-2)^{13}$$

17)
$$(3ab^7)^2$$

$$= (3)^{3}(a)^{3}(b^{7})^{3}$$

$$=9a^2b^{7x2}$$

Note: for #16 you will need the power of a quotient rule and #17 you will need the power of a product rule.

Summary of Exponent Laws

Product of Powers Rule	$x^a \cdot x^b = x^{a+b}$
Quotient of Powers Rule	$x^a \div x^b = x^{a-b}$
Power of a Power Rule	$(x^a)^b = x^{a \times b}$
Power of a Quotient	$\left(\frac{a}{b}\right)^x = \frac{a^x}{b^x}$
Power of a Product	$(ab)^x = a^x \cdot b^x$
Zero Exponent Rule	$x^0 = 1$
Negative Exponent Rule	$x^{-a} = \frac{1}{x^a}$