Section 4.7 - Combinations

many different handshakes would take place?

Ideas on how to solve the problem:

MDM4U Jensen

Guess: ____

Part 1: Handshake Problem

Problem: There are 26 students in this class. If every student shook every other students hand once, how

Part 2: Co	<u>mbinations</u>
PERMUTATIONS are ordered sets where: ABC/BCA permutations ORDER MATTERS.	/CAB etc. are all different possibilities, because with
HOWEVER, for many counting p	problems, order <u>is not</u> important!
COMBINATIONS are unordered sets where: ABC/BC combinations order DOES NOT matter.	CA/CAB etc. are considered the same, because with
Permutations	Combinations

Example 1:

You won four free tickets for the 2016 Stanley Cup Final (Pittsburgh vs. Edmonton....hopefully). Determine how many ways you can select 3 of your 10 best friends to come to the game with you.

before you start you must ask yourself, does the order you pick your friends really matter?

If yes --> permutation

If no --> combination

Example 3:

From a class of 30 students, determine how many ways a five-person committee can be selected to organize a class party:

a) With no restrictions



 $30 \rightarrow MATH \rightarrow PROB \rightarrow nCr \rightarrow 5 \rightarrow ENTER$

b) With Marnie on the committee

Example 4:

How many 5-card hands can be dealt out of a deck of 52 cards?

Note: $\binom{52}{5}$ means the same as C(52, 5)

Example 5:

A coach of a co-ed basketball team must select five players to start the game from a team that consists of six females and five males. How many ways can this be achieved if Tanya must choose three females and two males to start the game. (assume order does not matter)

Remember the Multiplication Rule for Counting:

To find the number of outcomes for a series of events, find the product of the possible outcomes at each step in the sequence.

$$n(a,b) = n(A) \times n(B)$$

Example 6:

In how many ways can 6 people be selected from a group that consists of four adults and eight children if the group must contain at least two adults?

Solution 1: Direct Reasoning

In this situation, the condition that the group must have at least two adults must be satisfied. This can happen three ways:

2 adults and 4 children or 3 adults and 3 children or 4 adults and 2 children

Remember the Additive Principle for the Union of Sets:

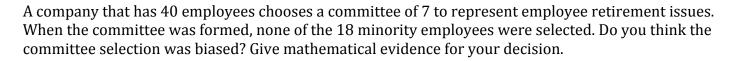
$$n(a \cup b) = n(A) + n(B)$$

(for disjoint sets)

Solution 2: Indirect Reasoning

In this situation, the solution can also be found by subtracting the number of ways the condition is not satisfied (0 or 1 adult in the group) from the total number of combinations.
Part 3: Using Combinations to Find Probabilities
Example 7:
Five cards are dealt at random from a deck of 52 playing cards. Determine the probability that you will have:
a) the 10-J-Q-K-A of the same suit (a royal flush)?
b) four of a kind?
Note: There are 13 cards in each suit and the hand must contain four of the same card. The remaining card in the hand can be any card of the remaining 48.

Example 8:



ъ	- 1			1			
۲o	SSI	n	e	SO	luti	on	1

Possible solution:
The number of ways 7 employees can be chosen from 40:
The number of ways 7 employees can be chosen from 22 non-minorities:
The probability that it contained no minorities if it was chosen randomly is: