L1 – Derivative of a Polynomial Functions MCV4U Jensen

In advanced functions, you should have been introduced to the idea that the instantaneous rate of change is represented by the slope of the \_\_\_\_\_\_ at a point on the curve. You also learned that you can determine this value by taking the derivative of the function using the Newton Quotient.

## Newton Quotient Example:

**a)** Find the equation of the derivative of  $f(x) = 3x^2 + 2x + 4$ 

Newton's Quotient:  $f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$ 

**b)** Calculate f'(5). What does it represent?



Mathematicians have derived a set of rules for calculating derivatives that make this process more efficient.

Rule	Derivative	Example
Constant Rule		
	f'(x) = 0	
If $f(x) = c$ where c is a constant		
Power Rule		
	$f'(x) = nx^{n-1}$	
If $f(x) = x^n$		
Constant Multiple Rule		
	$f'(x) = c \cdot a'(x)$	
If $f(x) = c \cdot g(x)$ where c is a	$\int (x) = c  g(x)$	
constant		
Sum Rule		
	h'(x) = f'(x) + g'(x)	
If $h(x) = f(x) + g(x)$		
Difference Rule		
	h'(x) = f'(x) - g'(x)	
If $h(x) = f(x) - g(x)$		

Proof of Power Rule:

Use Binomial Theorem:  
$$t_{r+1} = \binom{n}{r} a^{n-r} b^r$$

**Example 1:** Determine the equation of the derivative of each of the following functions:

**a)** 
$$f(x) = 3x^5$$
 **b)**  $f(x) = 71$  **c)**  $f(x) = \sqrt{x}$ 

**d**) 
$$y = \sqrt[3]{x}$$
 **e**)  $y = \frac{1}{x}$  **f**)  $y = -\frac{1}{x^5}$ 

Example 2: Differentiate each function

**a)** 
$$y = 5x^6 - 4x^3 + 6$$
  
**b)**  $f(x) = -3x^5 + 8\sqrt{x} - 9.3$ 

c) 
$$g(x) = (2x - 3)(x + 1)$$
  
d)  $h(x) = \frac{-8x^6 + 8x^2}{4x^5}$ 

**Example 3:** Determine an equation for the tangent to the curve  $f(x) = 4x^3 + 3x^2 - 5$  at x = -1.

Point on the tangent line:

Slope of tangent line:

**Remember:** The equation of the derivative tells you the slope of the tangent to the original function.

Equation of tangent line:

**Example 4:** Determine the point(s) on the graph of  $y = x^2(x + 3)$  where the slope of the tangent is 24.

