н :     	L2 – Maxima and Minima	Unit 2
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## Part 1: Review

Determine all local extrema for the function below using critical numbers and the first derivative test. State when the function is increasing and decreasing.

 $f(x) = 2x^3 + 3x^2 - 36x + 5$ 

**Remember:** Local extrema occur when the sign of the derivative CHANGES. If the sign of the derivative does not change, you have neither local extrema.

## Part 2: Local vs Absolute Extrema

Local max or min values of a function are also called local extrema or turning points.

**Local max:** If the *y*-coordinate of all points in the vicinity are less than the *y*-coordinate of the point. The sign of the derivative would change from positive before the point, to zero at the point, to negative after.

**Local min:** If the *y*-coordinate of all points in the vicinity are greater than the *y*-coordinate of the point. The sign of the derivative would change from negative before the point, to zero at the point, to positive after.

**Absolute max/min:** A function f(x) has an ABSOLUTE max or min at point a if f(a) is the biggest or smallest value of f(x) for ALL x in the domain.

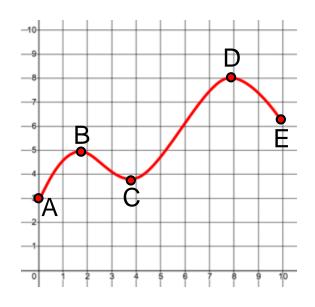
**Example 1:** Consider the graph of a function on the interval [0, 10].

a) Identify the local maximum points.

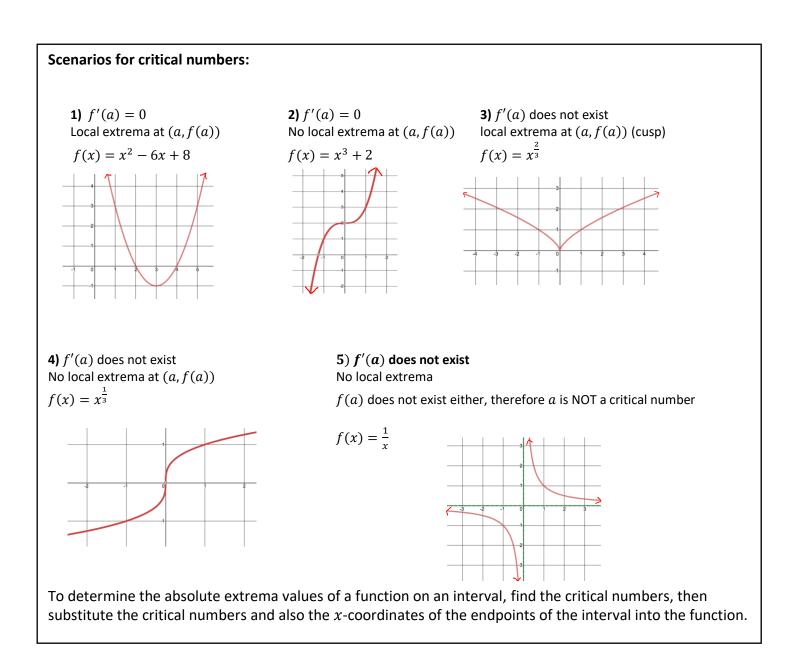
**b)** Identify the local minimum points.

**c)** What do all the points identified in parts a) and b) have in common?

**d)** Identify the absolute max and min points in the interval [0,10]



**Reminder:** A critical number of a function is a value of *a* in the domain of the function where either f'(a) = 0 or f'(a) does not exist. If *a* is a critical number, (a, f(a)) is a critical point.



**Example 2:** Find the absolute max and min of the function  $f(x) = x^3 - 12x - 3$  on the interval  $-3 \le x \le 4$ .

Test critical numbers AND endpoints of interval. **Example 3:** The surface area of a cylindrical container is to be 100  $cm^2$ . Its volume is given by the function  $V(r) = 50r - \pi r^3$ , where r is the radius of the cylinder in cm. Find the max volume of the cylinder if the radius cannot exceed 3 cm.