L4-5.3 Transformations of Trig Functions
MHF4U
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## Part 1: Transformation Properties

$$
y=a \sin [k(x-d)]+c
$$

## Desmos Demonstration

| $a$ | $k$ | $d$ | c |
| :---: | :---: | :---: | :---: |
| Vertical stretch or compression by a factor of $\|a\|$. <br> Vertical reflection if $a<0$ $\|a\|=\text { amplitude }$ | Horizontal stretch or compression by a factor of $\frac{1}{\|k\|}$. <br> Horizontal reflection if $k<0$. $\frac{2 \pi}{\|k\|}=\text { period }$ | Phase shift $\begin{aligned} & d>0 ; \text { shift right } \\ & d<0 ; \text { shift left } \end{aligned}$ | Vertical shift $\begin{aligned} & c>0 ; \text { shift up } \\ & c<0 ; \text { shift down } \end{aligned}$ |

Example 1: For the function $y=3 \sin \left[\frac{1}{2}\left(\theta+\frac{\pi}{3}\right)\right]-1$, state the...

| Amplitude: | Period: |
| :--- | :--- |
| Phase shift: | Vertical shift: |
|  |  |
| Max: | Min: |

## Part 2: Given Equation $\rightarrow$ Graph Function

Example 2: Graph $y=2 \sin \left[2\left(x-\frac{\pi}{3}\right)\right]+1$ using transformations. Then state the amplitude and period of the function.

| $y=\sin x$ |  |
| :--- | :--- |
| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |


| $y=2 \sin \left[2\left(x-\frac{\pi}{3}\right)\right]+1$ |  |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |



## Part 3: Given the Graph $\rightarrow$ Write the Equation

$y=a \sin [k(x-d)]+c$

| $a$ | $k$ | $d$ | $c$ |
| :--- | :--- | :--- | :--- |
| Find the amplitude of the <br> function: | Find the period (in radians) <br> of the function using a <br> starting point and ending <br> point of a full cycle. | for $\sin x: x$-coordinate of a <br> rising mid-line. <br> for $\cos x: x$-coordinate of a <br> maximum point. | Find the vertical shift |
| OR |  |  |  |

Example 3: Determine the equation of a sine and cosine function that describes the following graph


Example 4: Determine the equation of a sine and cosine function that describes the following graph


## Example 5:

a) Create a sine function with an amplitude of 7 , a period of $\pi$, a phase shift of $\frac{\pi}{4}$ right, and a vertical displacement of -3.
b) What would be the equation of a cosine function that represents the same graph as the sine function above?

| Even Functions | Odd Functions |
| :---: | :---: |
| EVEN FUNCTION if: <br> Line symmetry over the $\qquad$ | ODD FUNCTION if: <br> Point symmetry about the $\qquad$ |
| Rule: $f(-x)=f(x)$  | Rule: $-f(x)=f(-x)$  |
| Example: $y=\cos x$  | Example: |
|  | $y=\tan x$ is also an odd function |

