## Part 1: Investigation

$$
y=\sin x
$$



$$
y=\sin (2 x)
$$


a) What is the period of both of the functions above? How many cycles between 0 and $2 \pi$ radians?
b) Looking at the graph of $y=\sin x$, how many solutions are there for $\sin x=\frac{1}{\sqrt{2}} \approx 0.71$ ?
c) Looking at the graph of $y=\sin (2 x)$, how many solutions are there for $\sin (2 x)=\frac{1}{\sqrt{2}} \approx 0.71$ ?
d) When the period of a function is cut in half, what does that do to the number of solutions between 0 and $2 \pi$ radians?

Example 1: $\sin (2 \theta)=\frac{\sqrt{3}}{2}$ where $0 \leq \theta \leq 2 \pi$

Example 2: $\cos (2 \theta)=-\frac{1}{2}$ where $0 \leq \theta \leq 2 \pi$

Example 3: $\tan (2 \theta)=1$ where $0 \leq \theta \leq 2 \pi$

