# Unit 1 - Algebra

# Chapter 4 – Equations WORKBOOK

# MPM1D

## School Cartoon #6446

@ MARK ANDERSON

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"You knew X was 7 the whole time and you never said anything?!"

# **Chapter 4 Worksheet Checklist**

Worksheet	Check ✓
4.1 – Solving Simple Equations	
4.1 – Solving Simple Equations Worksheet #2	
4.2 – Solving Multi-Step Equations Worksheet #1	
4.2 Practice: Solve Multi-Step Equations	
Kuta – Multi-Step Equations (optional)	
4.3 – Solve Equations Involving Fractions #1	
4.3 – Solve Equations Involving Fractions #2	
4.4 – Modeling With Formulas Worksheet	
4.5 – Modeling With Algebra Worksheet #1	
4.5 Modeling With Algebra Practice	
Chapter 4 Review	
Chapter 4 Practice Test	

Mark	/10	0-2	3-5	6-8	9-10
Work compl	letion	Little to know	Some homework	Most homework	All homework
for chapter	4	homework done	completed.	completed. Work	completed
		throughout	Unorganized.	clear and	accurately. Great
		chapter.		organized.	organization of
					work.

Mark	/4	1	2	3	4
In Class Work	k for	Class time not used	Some work	Works well during	Always uses class
Chapter 4		well for work	completed during	class. Minimal	time efficiently.
		completion.	class. Sometimes	distractions. Good	Pays attention and
		Inattentive during	distracted during	attention during	contributes to
		lessons. Need to	lessons.	lessons.	lessons.
		improve at limiting			
		distractions.			

#### **Comments:**

#### 1. Solve the following equations:

a) 
$$x + 3 = 12$$

**b)** 
$$a + 4 = 7$$

**c)** 
$$y + 9 = 11$$

**d)** 
$$b + 5 = 14$$

**e)** 
$$m + 6 = 7$$

**f)** 
$$p - 4 = 2$$

**g)** 
$$h + 1 = 7$$

**h)** 
$$x + 8 = 12$$

**i)** 
$$m + 7 = 10$$

**j)** 
$$p + 5 = 6$$

**e)** 
$$r - 9 = 2$$

**f)** 
$$t - 3 = 5$$

# 2. Solve the following equations:

**a)** 
$$6w = 32$$

**b)** 
$$5y = 35$$

**c)** 
$$-2x = 18$$

**d)** 
$$\frac{k}{4} = 3$$

**b)** 
$$\frac{u}{2} = 8$$

**c)** 
$$\frac{r}{-5} = -2$$

#### MPM1D

#### 3. Solve each two-step equation

a) 
$$7x - 4 = 10$$

b) 
$$-12x - 36 = 0$$

c) 
$$-3x - 1 = 14$$

d) 
$$\frac{x}{-3} + 5 = 10$$

e) 
$$5 + \frac{x}{2} = -2$$

f) 
$$-3 + 8x = 1$$

# 4. A hockey team has \$700 to buy new jerseys. Ice-wear, a jersey supplier, charges \$50 per jersey. How many new jerseys can the team buy?

a) Write an equation that models the number of jerseys the team can afford.

**b)** Solve the equation. Write a conclusion to the problem.

#### **Answers**

#### 1. Solve

a) 
$$x - 5 = 4$$

b) 
$$m + 8 = 11$$

c) 
$$y - 3 = 0$$

d) 
$$h + 2 = 6$$

#### 2. Solve

a) 
$$x + 5 = 12$$

b) 
$$x - 6 = 7$$

c) 
$$y + 3 = 10$$

d) 
$$y - 4 = 2$$

#### 3. Solve

a) 
$$x + 7 = 12$$

b) 
$$n - 8 = 11$$

c) 
$$-5 + y = -2$$
 d)  $-9 + h = -6$ 

d) 
$$-9 + h = -6$$

#### 4. Solve

a) 
$$3x = 12$$

b) 
$$5y = 20$$

c) 
$$\frac{n}{3} = 8$$

d) 
$$-2k = 16$$

#### **5.** Solve

a) 
$$4z = -24$$

b) 
$$\frac{h}{-5} = -6$$

c) 
$$-6c = -42$$

d) 
$$-9u = 45$$

#### **6.** Find the root of each equation

a) 
$$7x - 4 = 10$$

b) 
$$7k + 2 = 16$$
 c)  $-p + 7 = 0$ 

c) 
$$-p + 7 = 0$$

d) 
$$-12g - 33 = 0$$

#### 7. Solve

a) 
$$k - 4 = -9$$

b) 
$$6x = -30$$

c) 
$$\frac{q}{7} = 2$$

d) 
$$2y - 7 = 9$$

e) 
$$-3w - 1 = 14$$

f) 
$$2q - 9 = -13$$

#### 8. Solve

a) 
$$p + 9 = -2$$

b) 
$$-5x = 35$$

c) 
$$\frac{u}{4} = -8$$

d) 
$$6r + 3 = 33$$

e) 
$$10c - 6 = -16$$

f) 
$$-3v + 6 = -9$$

- 9. At a bake sale, pies cost \$7 each. One customer buys \$84 worth of pies
- a) Write an equation to model the number of pies the customer bought.
- b) Solve the equation.

**12.** Solve each equation. Express fraction answers in lowest terms.

a) 
$$2k - 7 = -8$$

b) 
$$3x + 8 = 2$$

c) 
$$4m - 6 = 12$$

d) 
$$-9u + 8 = 23$$

**13.** Solve each equation. Express fraction answers in lowest terms.

a) 
$$8r - \frac{3}{2} = -15$$

b) 
$$-10h - 6 = -\frac{2}{5}$$

#### **Answers:**

#### 4.1 Solve Simple Equations, pages 186-195

1. a) 
$$x = 9$$

**b)** 
$$m = 3$$

c) 
$$y = 3$$

**d)** 
$$h = 4$$

2. a) 
$$x = 7$$

**b)** 
$$x = 13$$
 **c)**  $y = 7$ 

c) 
$$v = 3$$

**d)** 
$$y = 6$$

3. a) 
$$x = 5$$
  
4. a)  $x = 4$ 

**b)** 
$$n = 19$$

**b)** 
$$n = 19$$
 **c)**  $y = 3$  **b)**  $y = 4$  **c)**  $n = 24$ 

**d)** 
$$h = 3$$
 **d)**  $k = -8$ 

5. a) 
$$z = -6$$

**b)** 
$$h = 30$$

c) 
$$c = 7$$

**d)** 
$$u = -5$$

**6.** a) 
$$x = 2$$

b) 
$$k=2$$

c) 
$$p = 7$$

c) 
$$p = 7$$
 d)  $g = -\frac{11}{4}$ 

7. a) 
$$k = -5$$

**b)** 
$$x = -5$$
 **c)**  $q = 14$  **e)**  $w = -5$  **f)**  $q = -2$ 

c) 
$$q = 14$$
  
f)  $q = -2$ 

**6)** 
$$y = 8$$
  
**8. a)**  $p = -11$ 

**b)** 
$$x = -7$$

c) 
$$u = -32$$

e) 
$$c = -1$$

f) 
$$v = 5$$

a) 
$$7p = 84$$

**a)** 
$$50j = 700$$
 **b)** 14 jerseys

11. Step Explanation
$$3x - 8 = 7$$
 Given equation
$$3x - 8 + 8 = 7 + 8$$
 Add 8 to both sides.
$$3x = 15 \quad \text{Simplify by adding integers.}$$

$$\frac{3x}{3} = \frac{15}{3}$$
 Divide both sides by 3.
$$x = 5$$
 Divide integers to give the solution for x.

**12.** a) 
$$k = -\frac{1}{2}$$
 b)  $x = -2$ 

**b)** 
$$x = -2$$

c) m = 
$$\frac{9}{9}$$

c) 
$$m = \frac{9}{2}$$
 d)  $u = -\frac{5}{3}$ 

**13.** a) 
$$r = -\frac{27}{16}$$
 b)  $h = -\frac{14}{25}$ 

**b)** 
$$h = -\frac{14}{25}$$

# 4.2 - Solve Multi-Step Equations Worksheet #1

MPM1D Jensen

#### 1. Solve

a) 
$$3 + 4m + 5m = 21$$

b) 
$$16y - 8 - 9y = 27$$

c) 
$$46 = 2 - 8w - 3w$$

d) 
$$3d + 4 - 9d + 12 = 0$$

#### 2. Solve

a) 
$$5x + 9 = 3x + 7$$

b) 
$$-2u - 8 = 5u - 1$$

c) 
$$4y - 13 = -6y + 7$$

d) 
$$7 - 5m = -2 - 2m$$

3. Solve

a) 
$$0 = 14 - x + 6x - 9$$

b) 
$$11 - n + 3 = 3n + 3n$$

c) 
$$4t - 5 = 2t + 5$$

d) 
$$6k - 3 - 2k = k - 3$$

4. Find the root of each equation

a) 
$$2(x-2) = 4x - 2$$

b) 
$$4c + 3 = 3(c - 4)$$

c) 
$$6p + 4(8 - p) = 22$$

d) 
$$k = 2(11 - k) + 14$$

5. Find the root of each equation

a) 
$$2(x-3) + 3(x-2) = 18$$

b) 
$$4(y-1) - (y-5) = 10$$

c) 
$$2(c+2) = 5(c+1) - 7$$

d) 
$$3(t-4) = -2(t+3) + 14$$

9. Solve each equation. Express fraction answers in lowest terms.

a) 
$$3x - 8 = 7x + 10$$

b) 
$$3 + 10i = 4i - 18$$

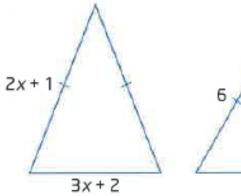
c) 
$$-4(u+6) = 2(3u-4)$$

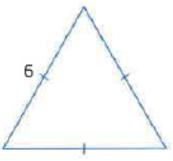
d) 
$$4(k-3) = 2 - (2k-6)$$

e) 
$$3(p+7) - (4p-1) = -5(2p-3) + 1$$

f) 
$$8 - (3w - 2) = -5(w - 3) - (4w - 3)$$

13. An isosceles triangle and an equilateral triangle have the same perimeter. Find the side lengths of each triangle.





Get Ready for Tomorrow:

17. Solve each equation

a) 
$$\frac{1}{2}(x+6) = 4(x-2)$$

b) 
$$\frac{1}{3}k + \frac{1}{2} = \frac{1}{4}k$$

#### **Answers:**

#### 4.2 Solve Multi-Step Equations, pages 196-203

1. a) 
$$m = 2$$

**b)** 
$$y = 5$$

c) 
$$w = -4$$

**1.** a) 
$$m = 2$$
 b)  $y = 5$  c)  $w = -4$  d)  $d = \frac{8}{3}$ 

2. a) 
$$x = -1$$

**b)** 
$$u = -1$$

$$c_{ij}y = a$$

$$d) k = d$$

3. a) 
$$x = -1$$

**b)** 
$$n = 2$$

c) 
$$t = 5$$

**d)** 
$$k = 0$$

2. a) 
$$x = -1$$
 b)  $u = -1$  c)  $y = 2$  d)  $m = 3$ 
3. a)  $x = -1$  b)  $n = 2$  c)  $t = 5$  d)  $k = 0$ 
4. a)  $x = -1$  b)  $c = -15$  c)  $p = -25$  d)  $k = 12$ 
5. a)  $x = 6$  b)  $y = 3$  c)  $c = 2$  d)  $t = 4$ 

**b)** 
$$c = -15$$

**d)** 
$$k = 1$$

5. a) 
$$x = 6$$

**b)** 
$$y = 3$$

c) 
$$c = 2!$$

**d)** 
$$t = 4$$

**9.** a) 
$$x = -\frac{9}{2}$$
 b)  $i = -\frac{7}{2}$  c)  $u = \frac{8}{5}$ 

**b)** 
$$i = -\frac{7}{2}$$

c) 
$$u = -\frac{8}{5}$$

d) 
$$k = \frac{10}{3}$$
 e)  $p = -\frac{2}{3}$  f)  $x = \frac{4}{3}$ 

e) 
$$p = -\frac{2}{3}$$

f) 
$$x = \frac{4}{3}$$

isosceles triangle: 5, 5, 8; equilateral triangle: 6, 6, 6

**17.** a) 
$$x = \frac{22}{7}$$
 b)  $k = -6$ 

**b)** 
$$k = -6$$

# 4.2 – Solve Multi-Step Equations Worksheet #2

#### MPM1D

Jensen

1. Solve.

**a)** 
$$6x + 3 + 2x = 19$$

**g)** 
$$9q + 2 - 8q - 13 = 0$$

**b)** 
$$10m - 3m + 8 = 43$$

**h)** 
$$8 - 3k + 5k = 0$$

c) 
$$4a + a + 9 = 44$$

a) 
$$3b + 4 = 2b + 6$$

**d)** 
$$15 - 3b + b = 3$$

**b)** 
$$7p - 18 = 3p - 2$$

**e)** 
$$2y + 4 + 3y = 9$$

c) 
$$2x + 4 = 5x - 5$$

**f)** 
$$7f - 12 + f = 20$$

**d)** 
$$8g + 3 = g + 10$$

e) 
$$6h - 5 = 2h + 3$$

**b)** 
$$2(a-8) + 3(a+6) = 17$$

**f)** 
$$4m - 9 = m + 7$$

c) 
$$3(2p+1) = 5(p+1)$$

**g)** 
$$5r - 6 = 2r + 3$$

**d)** 
$$5d = 4(d+2)$$

**h)** 
$$-3y + 15 = y - 13$$

e) 
$$2(3t+5)-4(2t-1)=6$$

3. Solve.

**a)** 
$$4(x-3) = 3x-7$$

**f)** 
$$5(k+3) = 2(4k+7) - 5$$

4. Solve, then check.

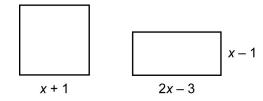
a) 
$$2m+1-m=4$$

**b)** 
$$q + 4 + 2q - 19 = 0$$

c) 
$$g-3+4g=2g-6$$

**d)** 
$$2(2b+7)=3(b+3)+3$$

**5.** A square and a rectangle have the same perimeter. Find the side lengths of each figure.



6. In a triangle, the measure of the middle angle is triple the measure of the smallest angle, and the measure of the largest angle is 55° greater than the measure of the smallest angle. Find the measures of the angles.

#### **ANSWERS**

- 1. a) 2
- **b**) 5
- **c)** 7
- **d)** 6

- e) 1 2. a) 2
- f) 4 b) 4
- g) 11 c) 3
- h) -4 d) 1

- **e)** 2
- f)  $\frac{16}{3}$
- **g**) 3
- **h)** 7

- 3. a) 5 d) 8
- b) 3e) 4

- c) 2f) 2
- **d)** -2
- 4. a) 3 b) 5 c) -1 5. square: 7; rectangle: 5 by 9 6. 25°, 75°, 80°

### **Two-Step Equations**

Solve each equation.

1) 
$$6 = \frac{a}{4} + 2$$

2) 
$$-6 + \frac{x}{4} = -5$$

3) 
$$9x - 7 = -7$$

4) 
$$0 = 4 + \frac{n}{5}$$

5) 
$$-4 = \frac{r}{20} - 5$$

6) 
$$-1 = \frac{5+x}{6}$$

7) 
$$\frac{v+9}{3} = 8$$

8) 
$$2(n+5) = -2$$

9) 
$$-9x + 1 = -80$$

10) 
$$-6 = \frac{n}{2} - 10$$

11) 
$$-2 = 2 + \frac{v}{4}$$

12) 
$$144 = -12(x+5)$$

-1-

13) 
$$-15 = -4m + 5$$

14) 
$$10 - 6v = -104$$

15) 
$$8n + 7 = 31$$

16) 
$$-9x - 13 = -103$$

17) 
$$\frac{n+5}{-16} = -1$$

18) 
$$-10 = -10 + 7m$$

19) 
$$-10 = 10(k-9)$$

20) 
$$\frac{m}{9} - 1 = -2$$

21) 
$$9 + 9n = 9$$

22) 
$$7(9+k) = 84$$

23) 
$$8 + \frac{b}{-4} = 5$$

24) 
$$-243 = -9(10 + x)$$

#### Date\_\_\_\_\_Period\_\_\_\_

#### **Two-Step Equations**

Solve each equation.

1) 
$$6 = \frac{a}{4} + 2$$
 {16}

$$2) -6 + \frac{x}{4} = -5$$

$$\{4\}$$

3) 
$$9x - 7 = -7$$
 {0}

4) 
$$0 = 4 + \frac{n}{5}$$
 {-20}

$$5) -4 = \frac{r}{20} - 5$$

$$\{20\}$$

$$6) -1 = \frac{5+x}{6}$$
$$\{-11\}$$

$$7) \ \frac{v+9}{3} = 8$$

$$\{15\}$$

8) 
$$2(n+5) = -2$$
 {-6}

9) 
$$-9x + 1 = -80$$
 {9}

$$10) -6 = \frac{n}{2} - 10$$

$$\{8\}$$

11) 
$$-2 = 2 + \frac{v}{4}$$
 {-16}

12) 
$$144 = -12(x+5)$$
  $\{-17\}$ 

-1-

13) 
$$-15 = -4m + 5$$
 {5}

14) 
$$10 - 6v = -104$$
 {19}

15) 
$$8n + 7 = 31$$
 {3}

16) 
$$-9x - 13 = -103$$
 {10}

$$17) \ \frac{n+5}{-16} = -1$$

$$\{11\}$$

18) 
$$-10 = -10 + 7m$$
 {0}

19) 
$$-10 = 10(k-9)$$
 {8}

$$20) \ \frac{m}{9} - 1 = -2$$
$$\{-9\}$$

21) 
$$9 + 9n = 9$$
 {0}

22) 
$$7(9+k) = 84$$
 {3}

23) 
$$8 + \frac{b}{-4} = 5$$
 {12}

24) 
$$-243 = -9(10 + x)$$
 {17}

# 4.3 - Solve Equations Involving Fractions Worksheet #1

MPM1D Jensen

1. Solve

a) 
$$\frac{1}{3}(x-2) = 5$$

b) 
$$4 = \frac{-2}{3}(p-2)$$

$$c)\frac{m+4}{3}=7$$

d) 
$$-14 = \frac{2(h-3)}{5}$$

2. Solve

a) 
$$\frac{y-4}{5} = -6$$

b) 
$$\frac{1}{4}(u-5) = -2$$

c) 
$$3 = \frac{2}{5}(n+7)$$

d) 
$$16 = \frac{3(v+7)}{2}$$

3. Find the root of each equation

a) 
$$\frac{m-3}{4} = \frac{m+1}{3}$$

b) 
$$\frac{w-1}{4} = \frac{w+2}{3}$$

c) 
$$\frac{1}{4}(x-3) = \frac{1}{3}(x-2)$$

d) 
$$\frac{1}{5}(y-3) = \frac{1}{6}(y+4)$$

4. Find the root of each equation.

a) 
$$\frac{2}{3}(5n-1) = -\frac{3}{5}(n+2)$$

b) 
$$-\frac{3}{4}(d+3) = \frac{4}{5}(3d-2)$$

c) 
$$\frac{3c-2}{5} = \frac{2c-1}{3}$$

d) 
$$\frac{5-2a}{4} = \frac{6-a}{5}$$

5. Each of the following solutions contains an error. Identify the error and describe how to correct it.

a) 
$$\frac{x-3}{5} = \frac{x+1}{4}$$

$$5(x-3) = 4(x+1)$$

$$5x-15 = 4x+4$$

$$5x-15-4x+15 = 4x+4-4x+15$$

$$x = 19$$

**b)** 
$$\frac{1}{3}(3y-2) = \frac{1}{4}(y+3)$$

$$12 \times \frac{1}{3}(3y-2) = 12 \times \frac{1}{4}(y+3)$$

$$3y-2 = y+3$$

$$3y-2-y+2 = y+3-y+2$$

$$2y = 5$$

$$\frac{2y}{2} = \frac{5}{2}$$

$$y = \frac{5}{2}$$

6. Find the height of a triangle with base 10 cm and area 50 cm<sup>2</sup>.

7. Solve

a) 
$$\frac{3p}{4} + \frac{p-5}{3} = \frac{1}{2}$$

b) 
$$\frac{u-3}{4} - 2 = \frac{3u}{2} + \frac{2u+1}{5}$$

#### **Answers**

1) a) 
$$x = 17$$
 b)  $p = -4$  c)  $m = 17$  d)  $h = -32$ 

2) a) 
$$y = -26$$
 b)  $u = -3$  c)  $n = \frac{1}{2}$  d)  $v = \frac{11}{3}$   
3) a)  $m = -13$  b)  $w = -11$  c)  $x = -1$  d)  $y = 38$   
4) a)  $n = \frac{-8}{59}$  b)  $d = \frac{-13}{63}$  c)  $c = -1$  d)  $a = \frac{1}{6}$ 

3) a) 
$$m = -13$$
 b)  $w = -11$  c)  $x = -1$  d)  $y = 38$ 

4) a) 
$$n = \frac{-8}{59}$$
 b)  $d = \frac{-13}{63}$  c)  $c = -1$  d)  $a = \frac{1}{6}$ 

- 5) a) The error is in the second line, 5(x-3)=4(x+1). The numerators on each side of the first line were multiplied by their own denominators. The correct step should be to multiply both sides by 20 (the LCD).
- b) The third line is incorrect. In the previous line, the denominators and the 12 were eliminated instead of being simplified. The third line should be 4(3y-2)=3(y+3)
- 6) 10 cm

7) a) 
$$p = 2$$
 b)  $u = \frac{-59}{33}$ 

# 4.3 – Solve Equations Involving Fractions Worksheet #2

#### MPM1D

Jensen

1. Solve.

**a)** 
$$\frac{c}{2} = 7$$

2. Find each root.

**a)** 
$$2 = \frac{1}{8}(s+7)$$

**b)** 
$$\frac{n}{-3} = 4$$

**b)** 
$$\frac{v+8}{5} = 4$$

**c)** 
$$\frac{w}{-3} = -5$$

**c)** 
$$\frac{3}{4}(r-1) = 6$$

**d**) 
$$\frac{h}{6} = -3$$

**d)** 
$$\frac{u-8}{2} = -1$$

e) 
$$-\frac{1}{4}(z-5) = -1$$

**d)** 
$$\frac{x+4}{3} = \frac{x+6}{5}$$

**f**) 
$$\frac{2(e+5)}{3} = -2$$

e) 
$$\frac{3n+2}{8} = \frac{3n-2}{4}$$

**a)** 
$$\frac{b+3}{4} = \frac{b-1}{2}$$

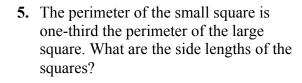
**f)** 
$$\frac{1}{9}(2y-1) = \frac{1}{3}(y+1)$$

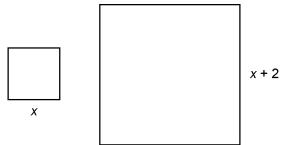
**b)** 
$$\frac{d-1}{6} = \frac{d-3}{3}$$

**a)** 
$$k-3 = \frac{k+3}{-5}$$

c) 
$$\frac{1}{6}(z-4) = \frac{1}{2}(z-2)$$

**b)** 
$$\frac{2z-3}{5} = 3$$





c) 
$$\frac{1}{3}(9+g)=g+1$$

**d)** 
$$\frac{h+2}{3} = \frac{3h-2}{5}$$

**6.** The height of a triangle is 2 cm less than its width. The area of the triangle is 24 cm<sup>2</sup>. What are the measures of the base and height?

# Answers

**1. a)** 14 **b)** -12

**c)** 15

**d)** -18

**2. a)** 9

**b)** 12

12 **c)** 9

9

**e)** 9

f) -8c) 1

3. a) 5 d) -1 4. a) 2

**d)** 6

b) 5e) 2

e) 2b) 9

**f**) -4

c) 3

**d)** 4

**5.** 1; 3

6. base: 8 cm; height: 6 cm

#### 4.4 - Modeling With Formulas Worksheet

#### MPM1D Jensen

**1.** Rearrange each formula to isolate the variable indicated.

a) 
$$P = 4s$$
 for  $s$ 

b) 
$$A = P + I$$
 for  $P$ 

c) 
$$C = 2\pi r$$
 for  $r$ 

c) 
$$y = mx + b$$
 for  $b$ 

**2.** Rearrange each formula to isolate the variable indicated.

a) 
$$d = mt + b$$
 for  $m$ 

b) 
$$P = 2l + 2w$$
 for  $w$ 

c) 
$$a = \frac{v}{t}$$
 for  $v$ 

d) 
$$v = \frac{d}{t}$$
 for  $t$ 

**3.** You can use the formula C=2.5I to obtain an approximate value for converting a length, I, in inches to a length, C, in centimetres.

- a) Use the formula to find the number of centimetres in
  - i) 6 inches

ii) 3 feet (1 foot = 12 inches)

b) Rearrange the formula to express *I* in terms of *C*.

- c) How man inches are in
  - i) 75 cm

ii) 1 m

<b>4.</b> Kwok is a hotel manager. His responsibilities include rentin \$250 per day plus \$15 per person for the grand ballroom.	ng rooms for conferences. The hotel charges
a) Create a formula that relates the cost, $\mathcal{C}$ , in dollars, of renting	ng the ballroom to the number of people, $n$ .
b) How much should Kwok charge to rent the hall for:	
i) 50 people	ii) 100 people
c) Rearrange your formula to express $n$ in terms of $\mathcal{C}$ .	
d) How many people could attend a wedding reception if the	wedding planners have a budget of:

**5.** The area, *A*, of a square is related to its perimeter, *P*, by the formula  $A = \frac{P^2}{16}$ 

a) Rearrange this formula to express P in terms of A.

ii) \$2000

i) \$4000

b) Find the perimeter of a square with area:
--

i) 
$$25 \text{ cm}^2$$
 ii)  $50 \text{ cm}^2$ 

**6.** Sometimes the same formula can have many different forms. PV = nRT is a useful formula in chemistry. It relates the characteristics of a gas:

Variable	Characteristic
Р	pressure
V	volume
R	universal gas constant
п	number of moles, or how much gas there is
Т	temperature

Rearrange this formula to isolate each variable:

**7.** The distance an accelerating object travels is related to its initial speed, v, its rate of acceleration, a, and time, t:

$$d = vt + \frac{1}{2}at^2$$

a) Rearrange this formula to isolate v.

b) An object travels 30 m while accelerating at a rate of 6 m/s<sup>2</sup> for 3 seconds. What was its initial speed?

#### **Answers:**

**1)** a) 
$$s = \frac{P}{4}$$
 b)  $P = A - I$  c)  $r = \frac{C}{2\pi}$  d)  $b = y - mx$ 

**2)** a) 
$$m = \frac{d-b}{t}$$
 b)  $w = \frac{P-2l}{2}$  c)  $v = at$  d)  $t = \frac{d}{v}$  e)  $r = \sqrt{\frac{A}{\pi}}$  f)  $I = \sqrt{\frac{P}{R}}$ 

**3)** a) i) 15 cm ii) 90 cm b) 
$$I = \frac{c}{2.5}$$
 c) i) 30 inches ii) 40 inches

**4)** a) 
$$C = 15n + 250$$
 b) i) \$1000 ii) \$1750 c)  $n = \frac{C - 250}{15}$  d) i) 250 ppl ii) 116 ppl

**5)** a) 
$$P = \sqrt{16A}$$
 b) i) 20 m ii) 28.3 m

**6)** 
$$P = \frac{nRT}{V}$$
;  $V = \frac{nRT}{P}$ ;  $n = \frac{PV}{RT}$ ;  $R = \frac{PV}{nT}$ ;  $T = \frac{PV}{nR}$ ;  $P = \frac{nRT}{V}$ 

**7)** a) 
$$v = \frac{d}{t} - \frac{at}{2}$$
 b) 1 m/s

# 4.5 Modeling With Algebra Worksheet #1

Jensen

1. Write an algebraic expression to represe	ent each description.
a) triple a number	
b) for more than a number	
c) half a number	
d) five less than double a number	
<b>2.</b> Write an equation to represent each sen	tence.
a) four times a number is 112	
b) a perimeter increased by 12 is 56	
c) five more than triple a number is 29	
d) the sum of two consecutive integers is 6	3
<b>3.</b> Solve each equation in question 2.	
a)	b)
c)	d)

<b>4.</b> Estaban is 6 years older than his brother Raoul. The sum of their ages is 38. How old are the brothers?
<b>5.</b> Two friends enter a trivia challenge as a team. Fayth scored 200 more points than Jamal. As a team, they collected a total of 2250 points. How many points did each friend earn?
6. Natalie, Chantal, and Samara play together as a forward line on a hockey team. At the end of the season, Chantal had scored eight more goals than Natalie while Samara had scored twice as many goals as Natalie. The three girls scored a total of 52 goals. How many goals did each girl score?
<b>7.</b> The sum of three consecutive integers is 54. Find the numbers.

$\bf 8.$ Paloma works part-time, 4 hours per day, selling fitness club memberships. She is paid \$9/h, plus a \$12 commission for each 1-year membership she sells.
a) Write an algebraic expression that describes Paloma's total earnings.
b) Find the amount Paloma makes in 8 hours when she sells 7 memberships.
c) How many memberships does Paloma need to sell to earn \$600 in a 24 hour work week?
<b>9.</b> The mass of a banana plus its peel is 360g. The mass of the banana is four times the mass of the peel. What is the mass of the peel?

#### **Answers**

1) a) 
$$3n$$
 b)  $n + 4$  c)  $\frac{1}{2}n$  d)  $2n - 5$ 

2) a) 
$$4n = 112$$
 b)  $p + 12 = 56$  c)  $3x + 5 = 29$  d)  $x + (x + 1) = 63$ 

8) a) 
$$E = 9h + 12m$$
 b) 156 c) 32

# **4.5 Modeling With Algebra Practice**

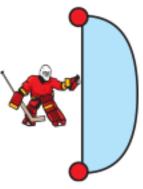
**Instructions:** Find an equation to represent each problem and then solve!

- 1. A box of fruit has four more apples than oranges. Together there are 52 pieces of fruit. How many of each type of fruit are there?
- 2. Thu and Cleo are sharing the driving on a 520 mile trip. If Thu drives 60 miles more than Cleo, how far did each of them drive?
- 3. Aimee cut a string that was originally 126 centimeters long in to two pieces so that one piece is twice as long as the other. How long is each piece?
- 4. A full bucket of water weighs eight kilograms. If the water weighs five times as much as the empty bucket, how much does the water weigh?
- 5. The perimeter of a rectangle is 100 feet. If the length is five feet more than twice the width, find the length and width.
- 6. The perimeter of a rectangular city is 94 miles. If the length is one mile less than three times the width, find the length and width of the city.
- 7. Find three consecutive numbers whose sum is 138.
- **8.** Find three consecutive even numbers whose sum is 468.
- 9. The perimeter of a triangle is 57. The first side is twice the length of the second side. The third side is seven more than the second side. What is the length of each side?
- 10. The perimeter of a triangle is 86 inches. The largest side is four inches less than twice the smallest side. The third side is 10 inches longer than the smallest side. What is the length of each side?

- 11. Thirty more student tickets than adult tickets were sold for the game. Student tickets cost \$2, adult tickets cost \$5, and \$1460 was collected. How many of each kind of ticket were sold?
- 12. Fifty more "couples" tickets than "singles" tickets were sold for the dance. "Singles" tickets cost \$10 and "couples" tickets cost \$15. If \$4000 was collected, how many of each kind of ticket was sold?
- 13. Helen has twice as many dimes as nickels and five more quarters than nickels. The value of her coins is \$4.75. How many dimes does she have?
- 14. Ly has three more dimes than nickels and twice as many quarters as dimes. The value of his coins is \$9.60. How many of each kind of coin does he have?
- 15. Enrique put his money in the credit union for one year. His money earned 8% simple interest and at the end of the year his account was worth \$1350. How much was originally invested?
- **16.** Juli's bank pays 7.5% simple interest. At the end of the year, her college fund was worth \$10,965. How much was it worth at the start of the year?

**Bonus:** Sidney is directly in front of Marc-Andre, who is playing goalie, as shown. Sidney is 2.8 m from both goal posts. He is also three times as far from Marc-Andre as Marc-Andre is from either post. How wide is the net?





### **SOLUTIONS:**

#### **Answers** (equations may vary)

- 1. 24oranges, 28 apples; x+(x+4)=52, x= oranges
- 2. Cleo230miles, Thu 290miles; x+(x+60)=520, x=Cleo
- 3. 42,84; x+2x=126, x=short piece
- 4. 6.7 kg.; x+5x=8, x=weight of bucket
- 5. 15,35; 2x+2(2x+5)=100, x= width
- 6. 12,35; 2x+2(3x-1)=94, x= width
- 7. 45,46,47;x+(x+1)+(x+2)=138 x = first number
- 8. 154,156,158; x+(x+2)+(x+4)=468 x = first number
- 9. 25,12.5,19.5;x+2x+(x+7)=57 x = second side
- 10. 20,36,30; x+(2x-4)+(x+10)=86 x = smallest side
- 11. 200 adult, 230 students; 5x + 2(x + 30) = 1460, x = adult tickets
- 12. 130 single, 180 couple; 10x + 15(x + 50) = 4000, x = "singles" tickets
- 13. 7 nickels, 14 dimes, 12 quarters; 0.05x + 0.10(2x) + 0.25(x + 5) = 4.75, x = nickels
- 14. 12 nickels, 15 dimes, 30 quarters; 0.05x + 0.10(x + 3) + 0.25(2x + 6) = 9.60, x = nickels
- 15. \$1250; x + 0.08x = 1350 16. 10,200; x + 0.075x = 10,965 x = amount invested x = original value of her fund
- 16. \$10200; 1.075x = 10965, x = amount invested