

**W4 – Limits**

MHF4U

Jensen

**1) Evaluate each limit**

**a)**  $\lim_{x \rightarrow 2} \frac{3x}{x^2 + 2}$

**b)**  $\lim_{x \rightarrow -1} (x^4 + x^3 + x^2)$

**c)**  $\lim_{x \rightarrow 9} \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right)^2$

**2) Evaluate the limit of each**

**a)**  $\lim_{x \rightarrow 2} \frac{4-x^2}{2-x}$

**b)**  $\lim_{x \rightarrow -1} \frac{2x^2+5x+3}{x+1}$

**c)**  $\lim_{x \rightarrow 3} \frac{x^3-27}{x-3}$

**d)**  $\lim_{x \rightarrow 4} \frac{16-x^2}{x^3+64}$

**e)**  $\lim_{x \rightarrow 4} \frac{x^2-16}{x^2-5x+6}$

**f)**  $\lim_{x \rightarrow -1} \frac{x^2+x}{x+1}$

**3) Complete the following table and use results to estimate  $\lim_{x \rightarrow 2} \frac{x-2}{x^2-x-2}$** 

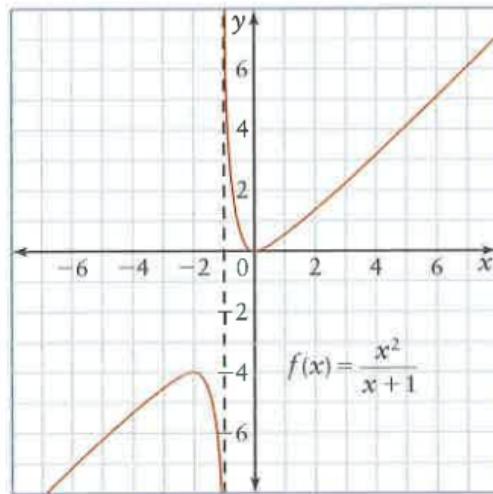
<b>x</b>	1.9	1.99	1.999	2.001	2.01	2.1
$\frac{x-2}{x^2-x-2}$						

4) Use the graph to find the following limits:

a)  $\lim_{x \rightarrow -1^+} \frac{x^2}{x+1}$

b)  $\lim_{x \rightarrow -1^-} \frac{x^2}{x+1}$

c)  $\lim_{x \rightarrow -1} \frac{x^2}{x+1}$



5) Use the graph to determine the following limits

a)  $\lim_{x \rightarrow -1^+} h(x)$

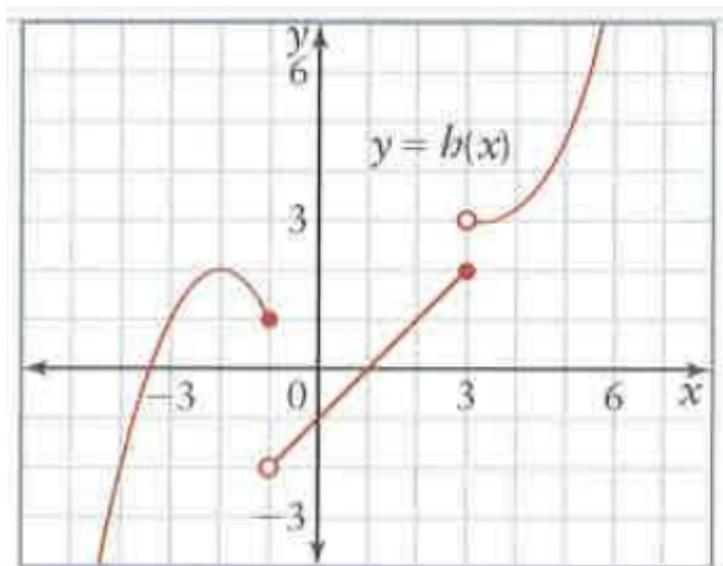
b)  $\lim_{x \rightarrow -1^-} h(x)$

c)  $\lim_{x \rightarrow -1} h(x)$

d)  $\lim_{x \rightarrow 3^+} h(x)$

e)  $\lim_{x \rightarrow 3^-} h(x)$

f)  $\lim_{x \rightarrow 3} h(x)$



### Answer Key

- 1)a) 1 b) 1 c)  $\frac{100}{9}$  2)a) 4 b) 1 c) 27 d) 0 e) 0 f) -1 3)  $\frac{1}{3}$  4)a)  $\infty$  b)  $-\infty$  c) does not exist  
5)a) -2 b) 1 c) does not exist d) 3 e) 2 f) does not exist